



Study of the response of the CALICE Si-W ECAL physics-prototype to positrons

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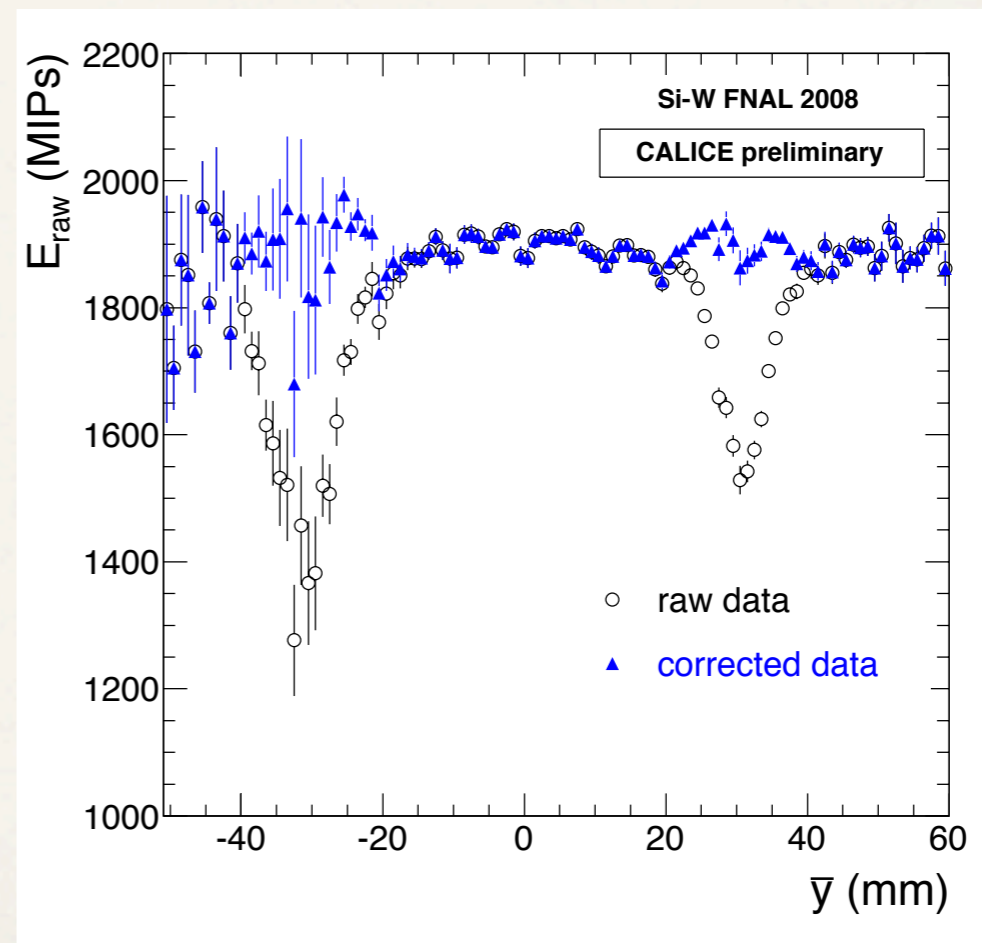
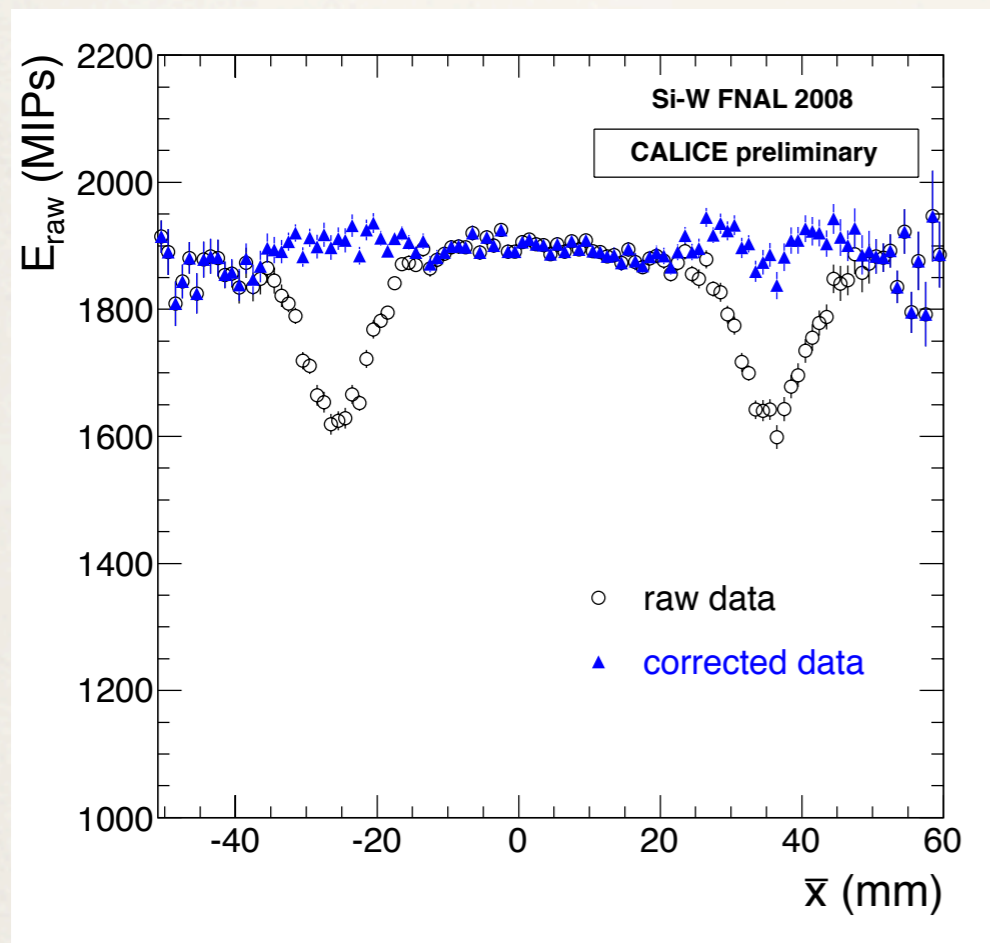
- ❖ Motivation
- ❖ Update of calibration constant
 - energy linearity, energy resolution
- ❖ Monte Carlo simulation
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 - shower distance to the gap
 - MIP threshold
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Motivation

- ❖ The CALICE Si-W ECAL physics prototype was constructed and tested.
 - the first beam test was conducted at CERN in 2006 using electron beams (6-45 GeV).
 - the second beam test was conducted at FNAL in 2008 using positron beams (4-20 GeV).
- ❖ We analyzed the prototype test beam data taken at FNAL in 2008.
- ❖ We want to evaluate linearity and energy resolution for positrons and to compare the prototype response to positrons and electrons.

Update of Calibration Constant

- ❖ There was mis-calibration in the bottom slab's modules.
→ We re-reconstructed the data with new calibration constants and rechecked the energy linearity and resolution.



Performance Study

❖ We rechecked the energy linearity and resolution.

- **energy resolution**

stochastic term :

$$16.51 \pm 0.35(\text{stat.})\% \rightarrow 16.67 \pm 0.30(\text{stat.})\%$$

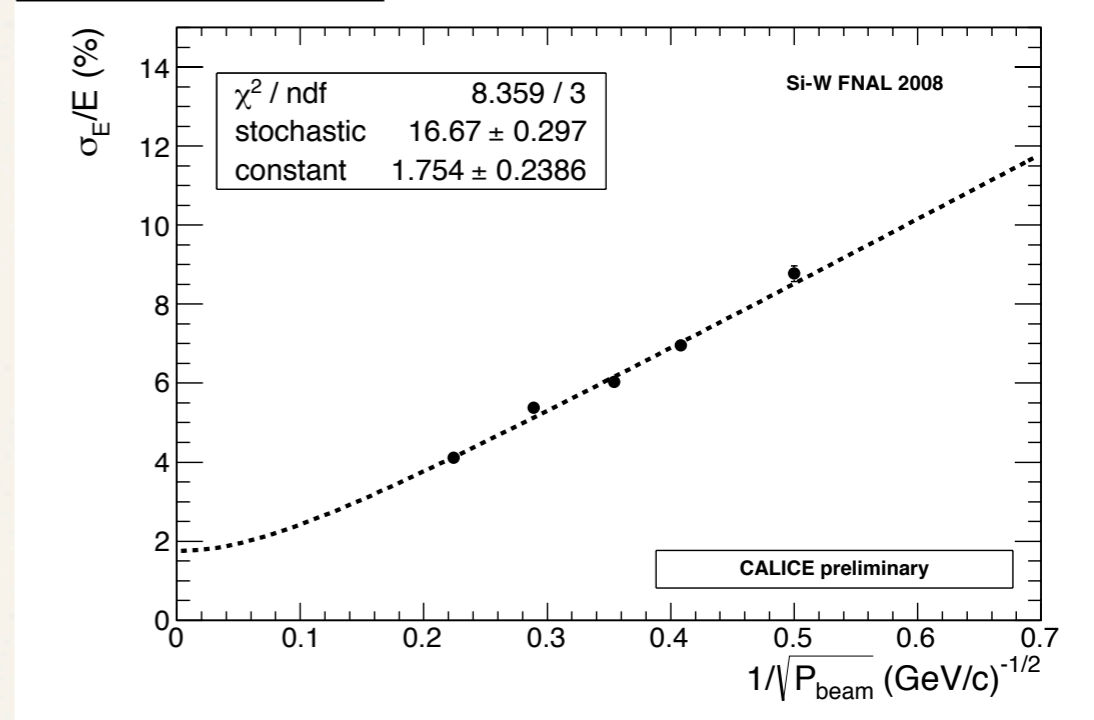
constant term:

$$1.90 \pm 0.15(\text{stat.})\% \rightarrow 1.75 \pm 0.24(\text{stat.})\%$$

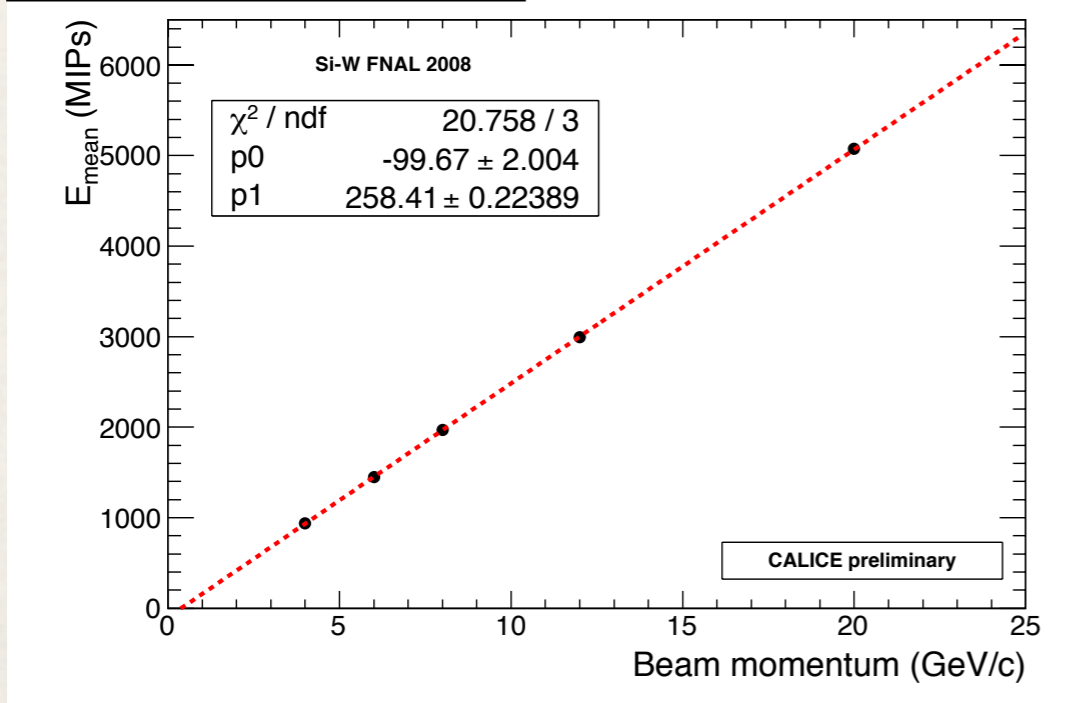
- **energy linearity**

the deviations from linear function is less than 0.5 %

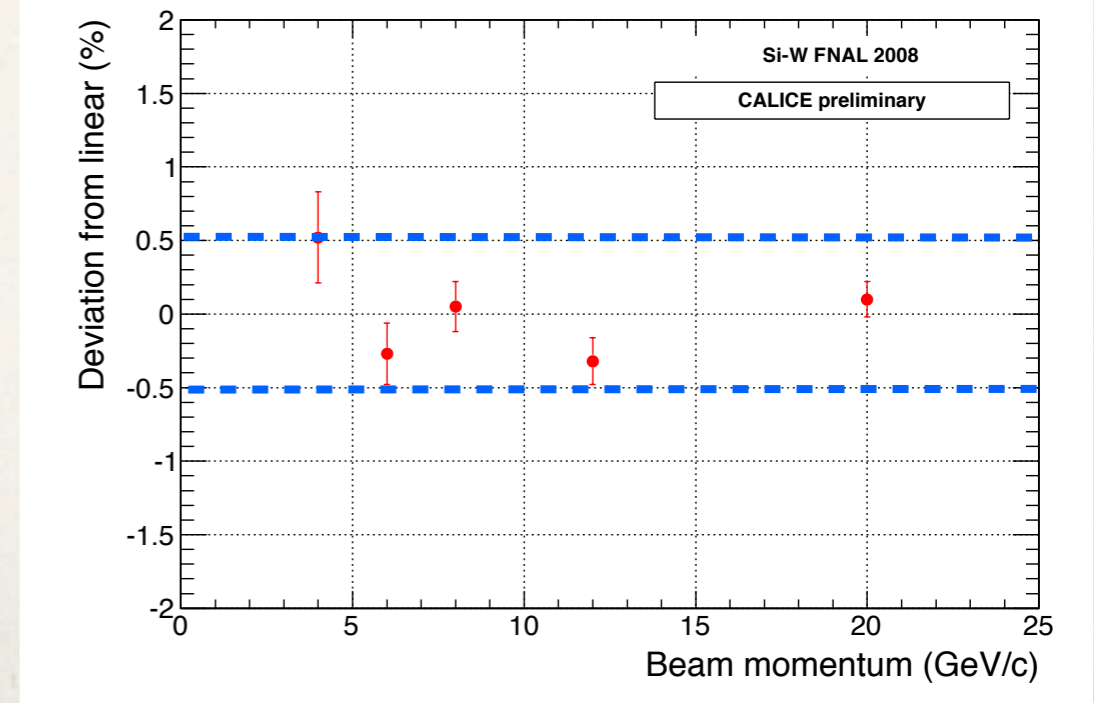
Energy resolution



Response of the linearity



Deviations from linear function



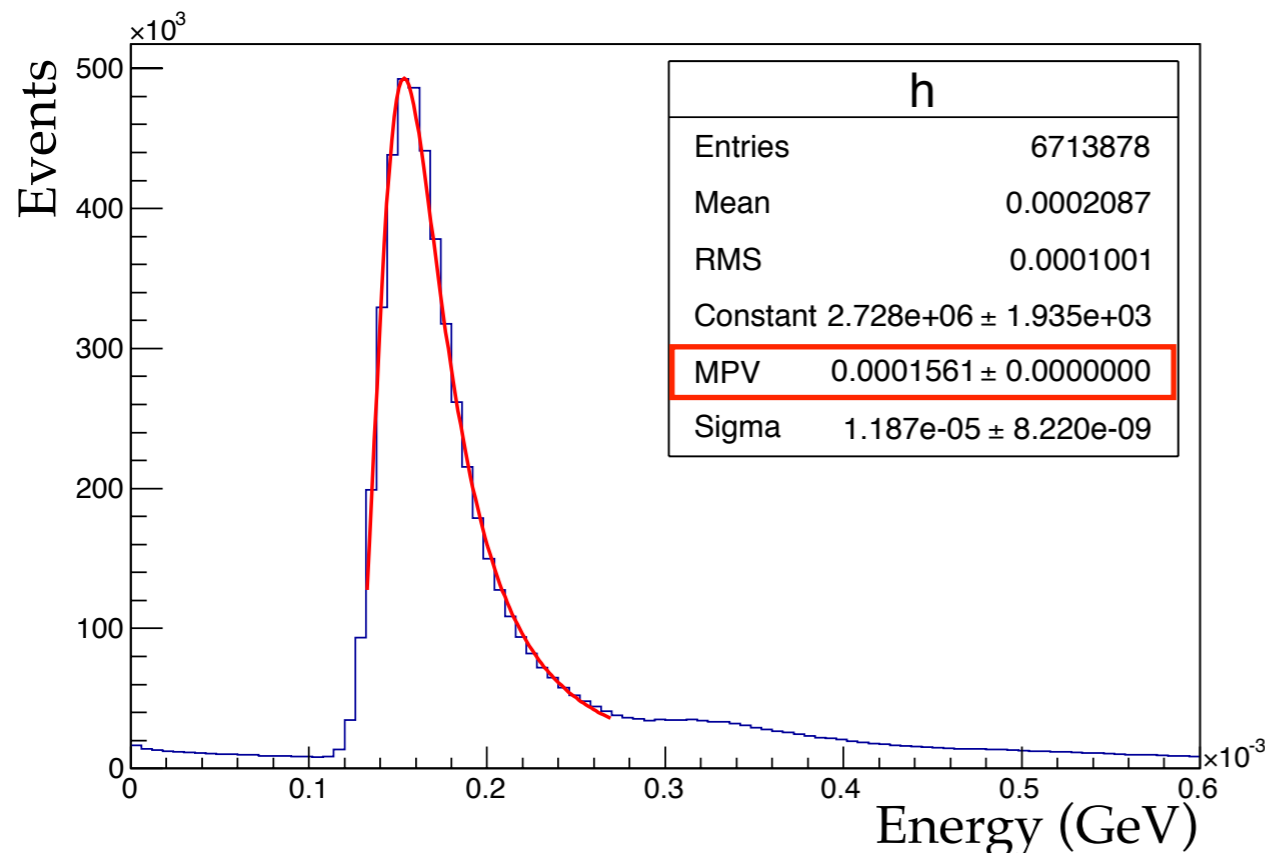
MC Simulation

* Analysis setup

- calice soft : v04-07
- ilcsoft : v01-17-03
- Mokka Detector Model : TBFnal0508_p0709

* MIP Calibration : 32 GeV muon

fitted with the landau function and extracted the MPV value.



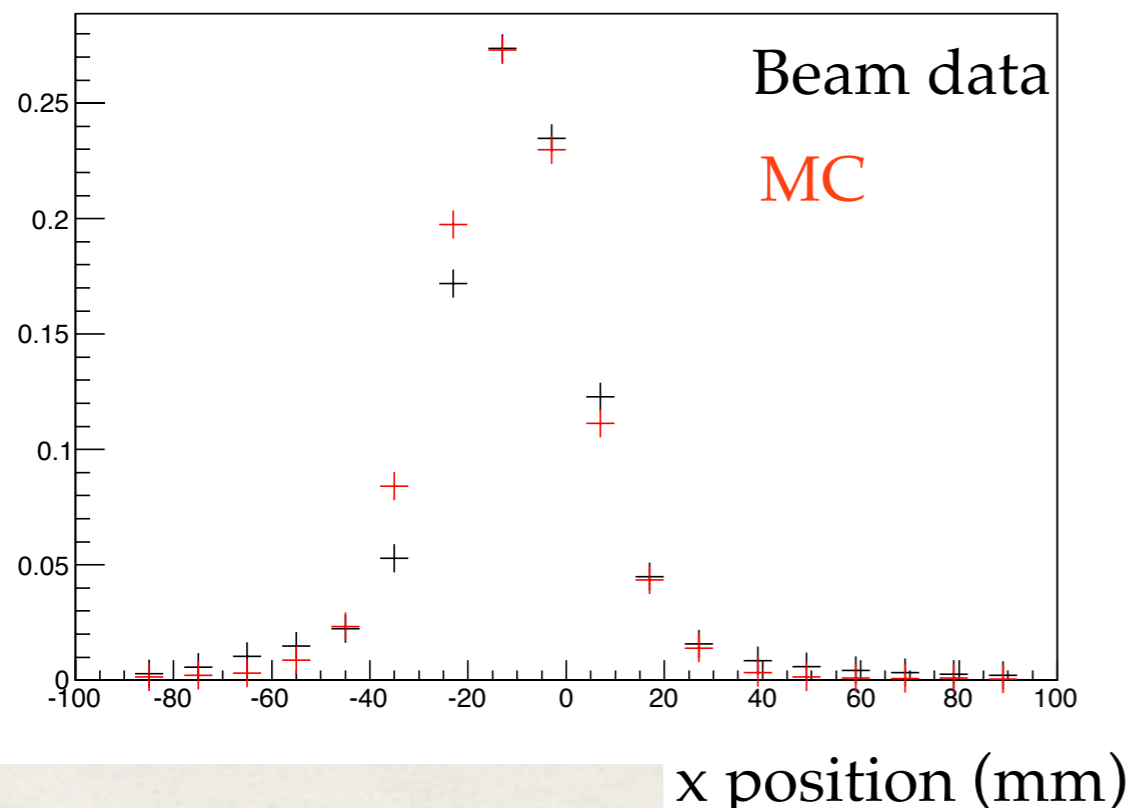
GeV to MIP conversion factor

$$1 \text{ MIP} = 0.000156 \text{ GeV}$$

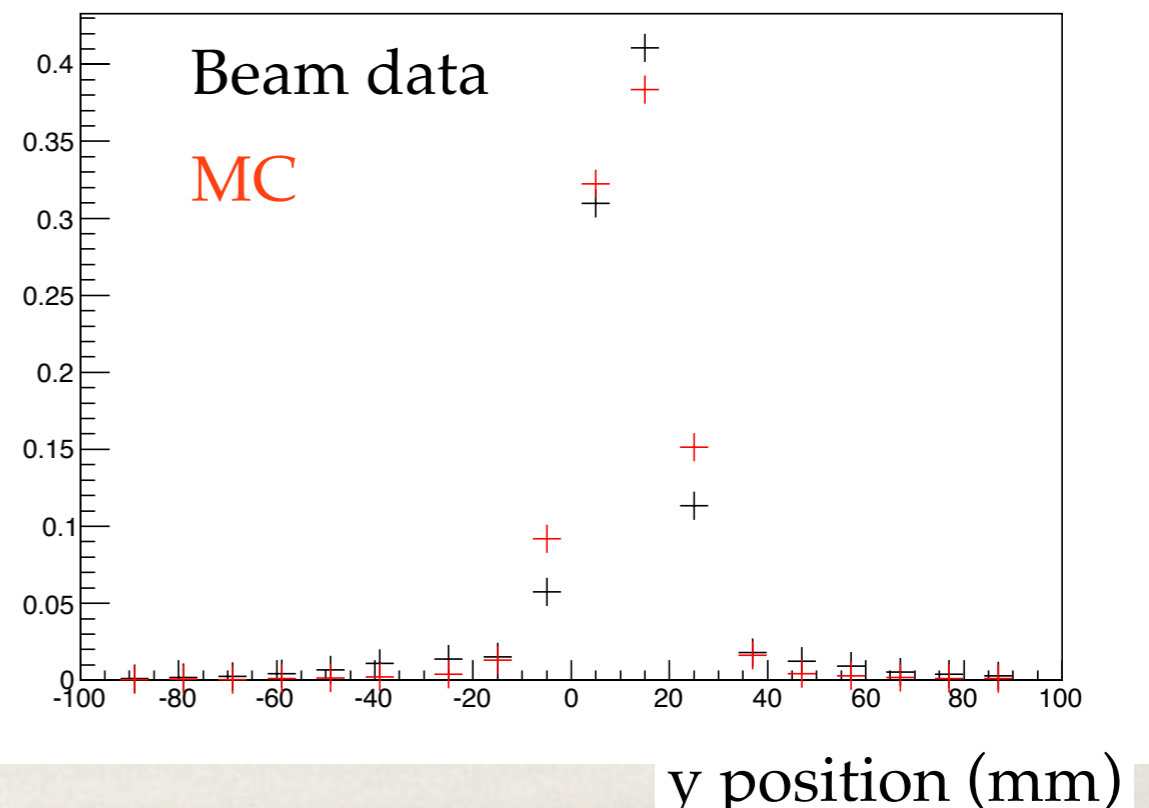
Beam Position

- ❖ We adjusted beam position of MC to that of the beam data by using single hit in a first layer.
- ❖ Beam momentum spread
 - 2.7% for 4, 6 GeV
 - 2.3% for 8, 12, 20 GeV

20 GeV 1st layer

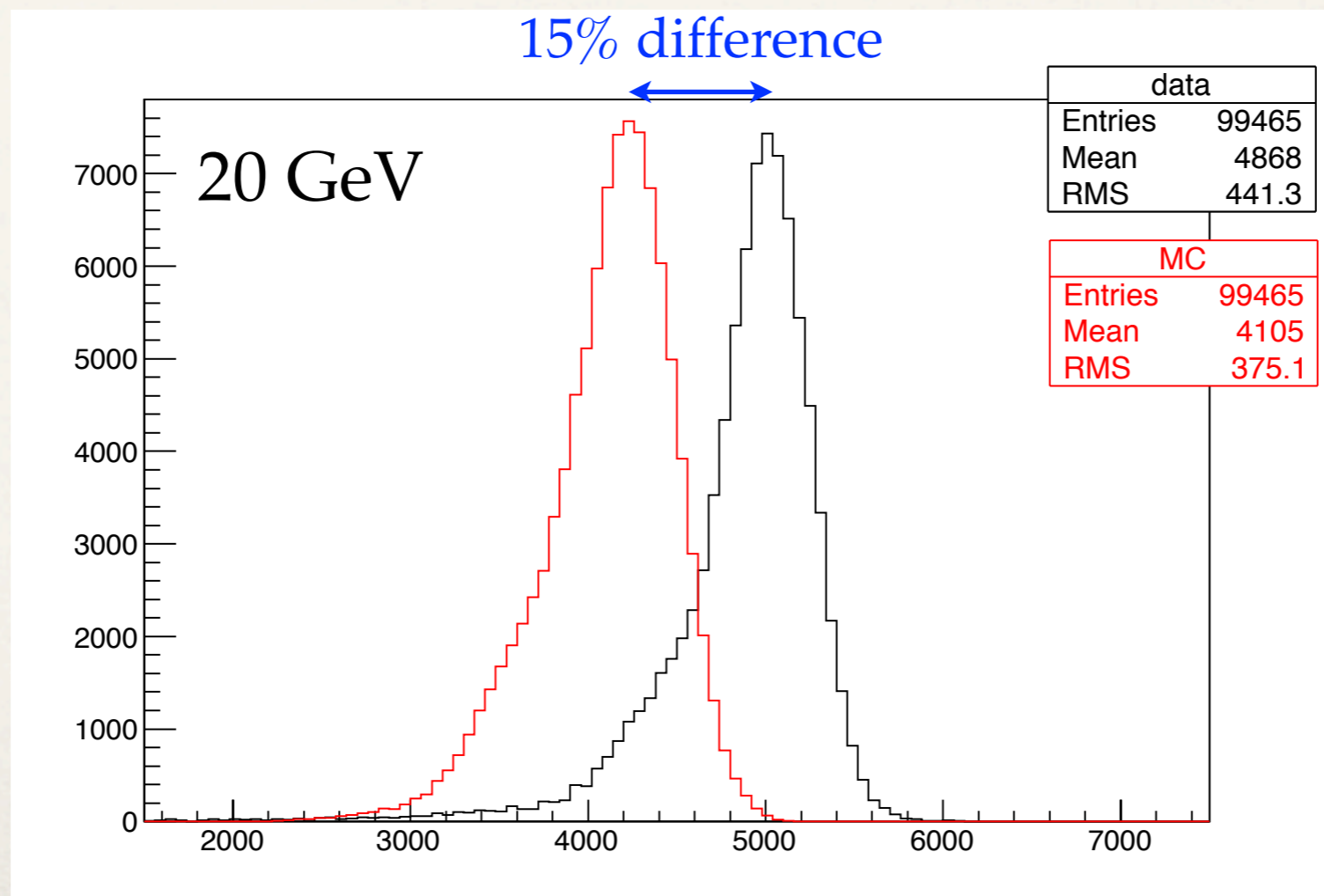


20 GeV 1st layer



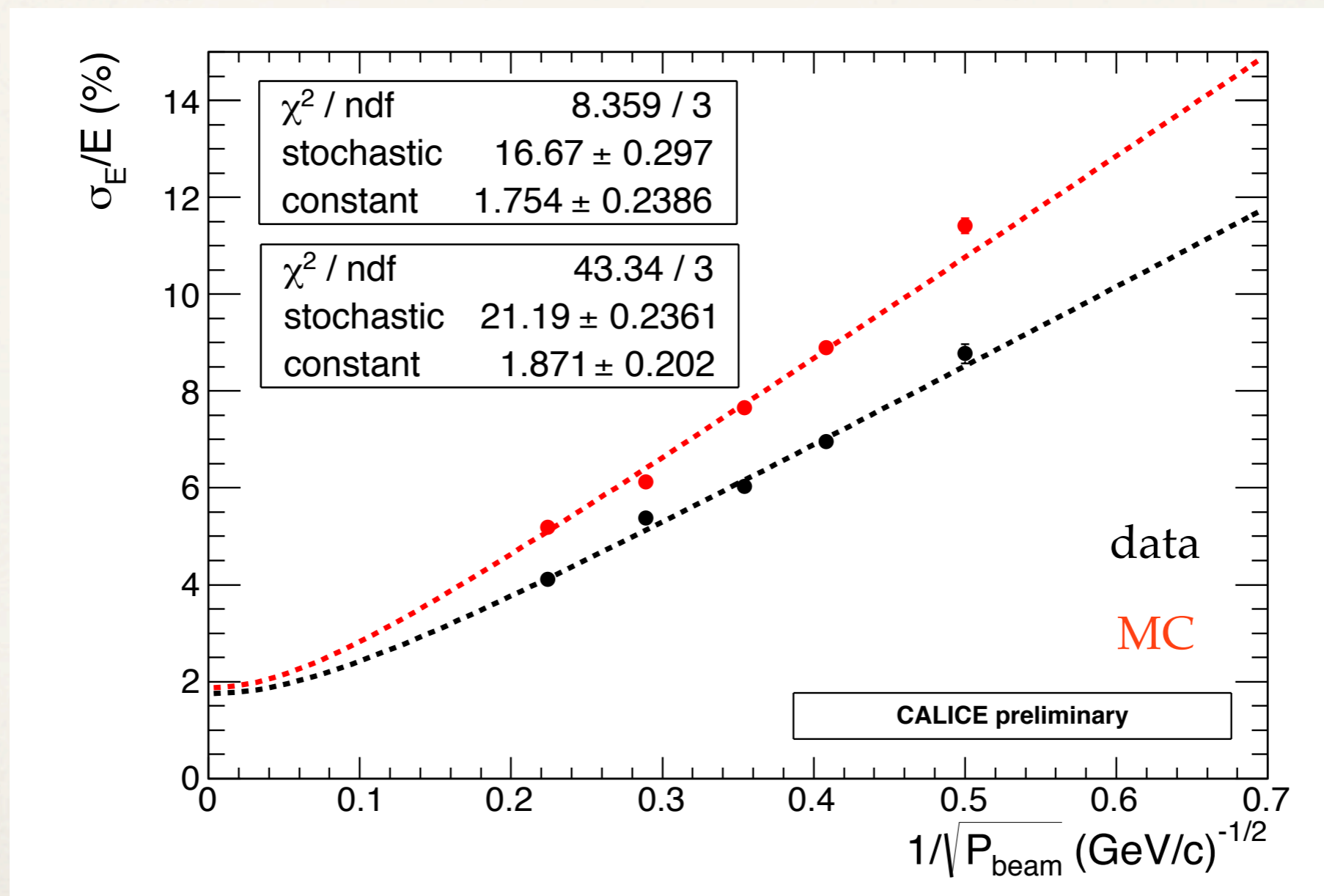
MC result

- ❖ We compared a energy distribution of MC with that of the test beam data.
- ❖ A mean of the MC is about 15% lower than that of test beam data and distribution is wider.
→ We scaled up the MC and adjust the mean value.



MC results

- ❖ We compared a energy resolution of the MC with that of the data.
 - There is 5% difference on stochastic term between data and MC
- ❖ The reason is now under investigation.



Systematic Error

- * Example of the systematic error of the energy resolution.
 - shower distance to the gaps
 - * distance between the barycenter and the nearest inter-wafer gaps.
 - * We checked the effect of varying this distance : $4\sigma \rightarrow 3\sigma, 3.5\sigma, 4.5\sigma$
 - MIP threshold
 - binning

shower distance to the gaps (in standard deviations)				
	3σ	3.5σ	4σ	4.5σ
χ^2/ndf	5.51/3	6.31/3	8.40/3	8.67/3
stochastic term (%)	16.74 ± 0.24	16.44 ± 0.25	16.67 ± 0.30	16.48 ± 0.36
constant term (%)	2.04 ± 0.17	2.09 ± 0.17	1.75 ± 0.24	1.79 ± 0.30

Systematic Error

- ❖ Example of the systematic error of the energy resolution.
 - shower distance to the gaps
 - **MIP threshold**
 - ❖ In this study, the energy threshold for considering the hits is 0.5 MIPs
 - ❖ We checked the effect of varying this threshold : 0.5 MIPs → 0.7 MIPs, 0.9 MIPs
 - binning

	MIP threshold		
	0.5 MIPs	0.7 MIPs	0.9 MIPs
χ^2 / ndf	8.40 / 3	9.16 / 3	5.42 / 3
stochastic term (%)	16.67±0.30	16.52±0.32	16.53±0.29
constant term (%)	1.75±0.24	1.77±0.27	1.90±0.21

Systematic Error

- ❖ Example of the systematic error of the energy resolution.
 - shower distance to the gaps
 - MIP threshold
 - **binning**
 - ❖ In order to investigate the effect of the width of the bin, we changed it.

binning		
	double	half
χ^2 / ndf	8.46 / 3	5.61 / 3
stochastic term (%)	16.33±0.30	16.66±0.28
constant term (%)	1.88±0.22	1.81±0.23

Systematic Error

- ❖ We estimated the systematic error of the energy resolution by quadratic sum.

stochastic term $16.67 \pm 0.30(\text{stat.})^{+0.07}_{-0.44}(\text{syst.})\%$

constant term $1.75 \pm 0.24(\text{stat.})^{+0.39}_{-0.00}(\text{syst.})\%$

- ❖ We didn't take a momentum spread into account in this estimation.
 - We need to add the effect of a beam momentum spread.

Summary

- ❖ We re-reconstructed the data with a new calibration constants
 - **energy linearity**
the deviations from linear function is less than 0.5 %
 - **energy resolution**
energy resolution changes little bit
- ❖ We performed a MC simulation
 - There was large difference between data and MC
 - The reason is now under investigation
- ❖ We estimated the systematic error of the energy resolution.
 - stochastic term** $16.67 \pm 0.30(\text{stat.})_{-0.44}^{+0.07}(\text{syst.})\%$
 - constant term** $1.75 \pm 0.24(\text{stat.})_{-0.00}^{+0.39}(\text{syst.})\%$

back up

Physics Prototype Design

Prototype Design

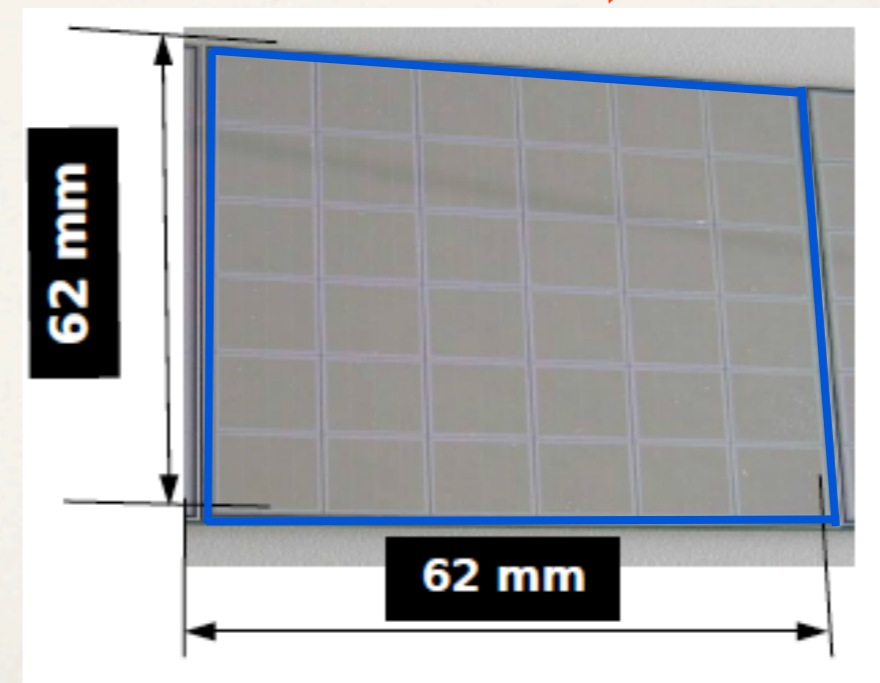
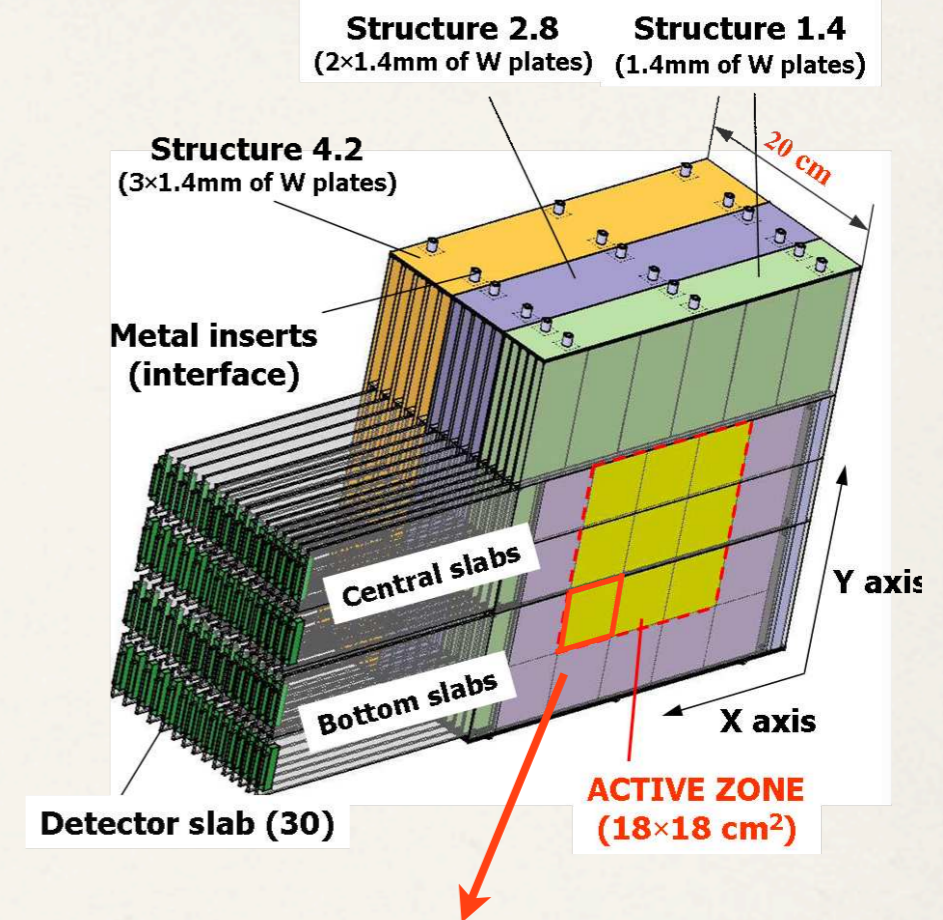
❖ The physics prototype consists of thirty sensitive layers and absorber layers.

- sensitive layer : silicon

- 6×6 pixels for one module
 - 3×3 modules in a layer (18×18 cm²)
- ➔ Total 9720 channels

- absorber layer : tungsten

- Structure 1.4 : 1-10 layer 1.4 mm (0.4X₀)
 - Structure 2.8 : 11-20 layer 2.8 mm (0.8X₀)
 - Structure 4.2 : 21-30 layer 4.2 mm (1.2X₀)
- ➔ Total 24X₀

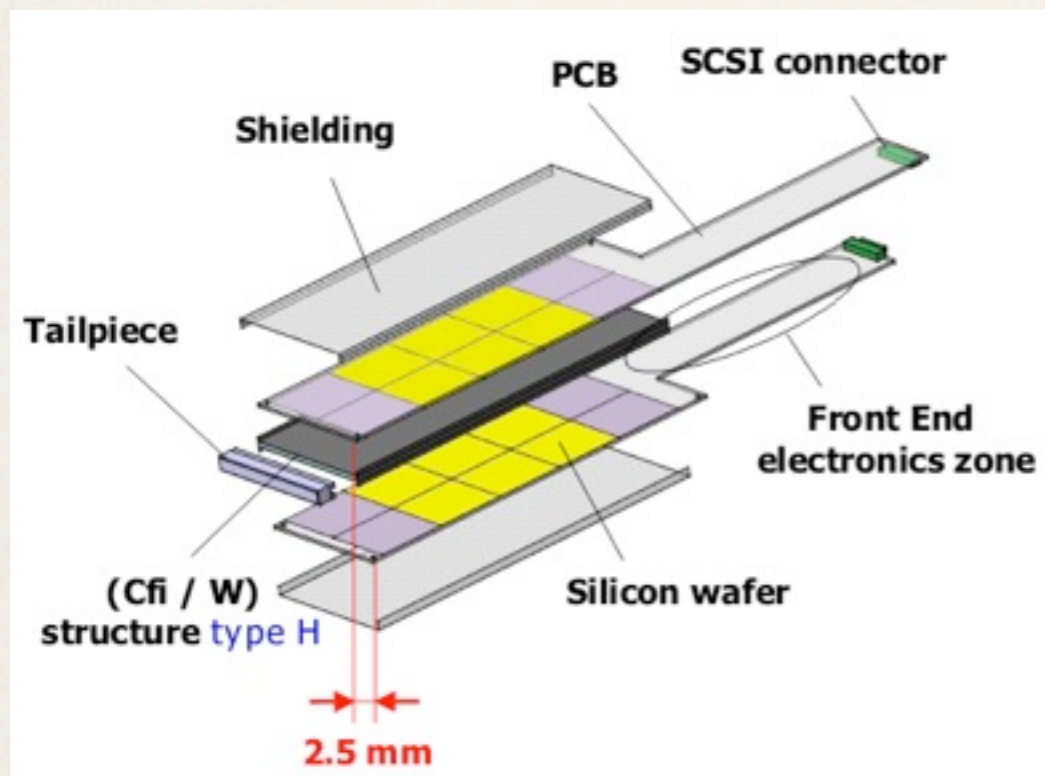


Silicon sensor

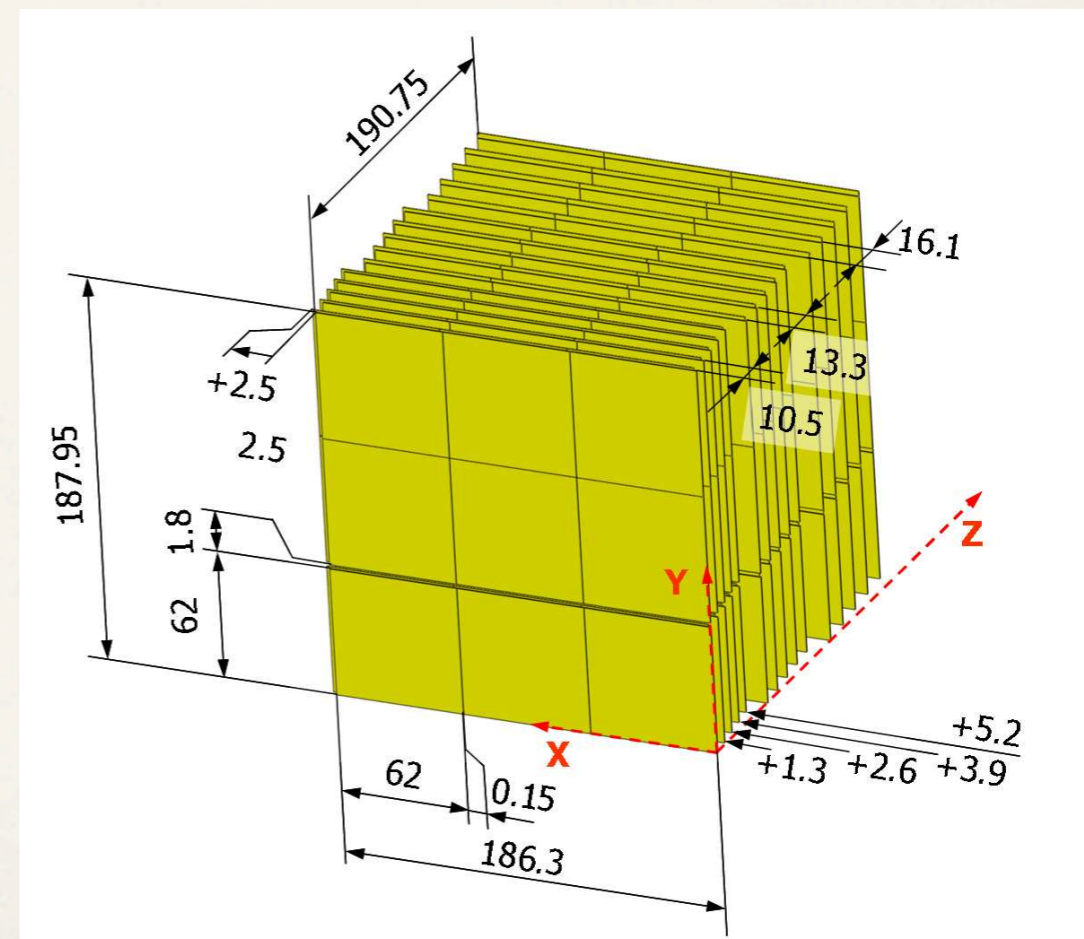
Thickness:
525 μm
pixel size:
10 mm
guard ring
1 mm

Details of the passive area and offsets

- ❖ There is an inactive area in an active layer due to 1 mm guard ring around the modules.
- ❖ In order to reduce their overlapping, the two layers are offset by **2.5 mm** in the x direction (no offset in the y direction)



Detector slab



Test Beam @FNAL in 2008

- ❖ The CALICE ECAL prototype was tested at FNAL MTest area in 2008.
 - 4, 6, 8, 12 and 20 GeV positron beams

The analog HCAL was located behind the ECAL

➡ hit number information is available

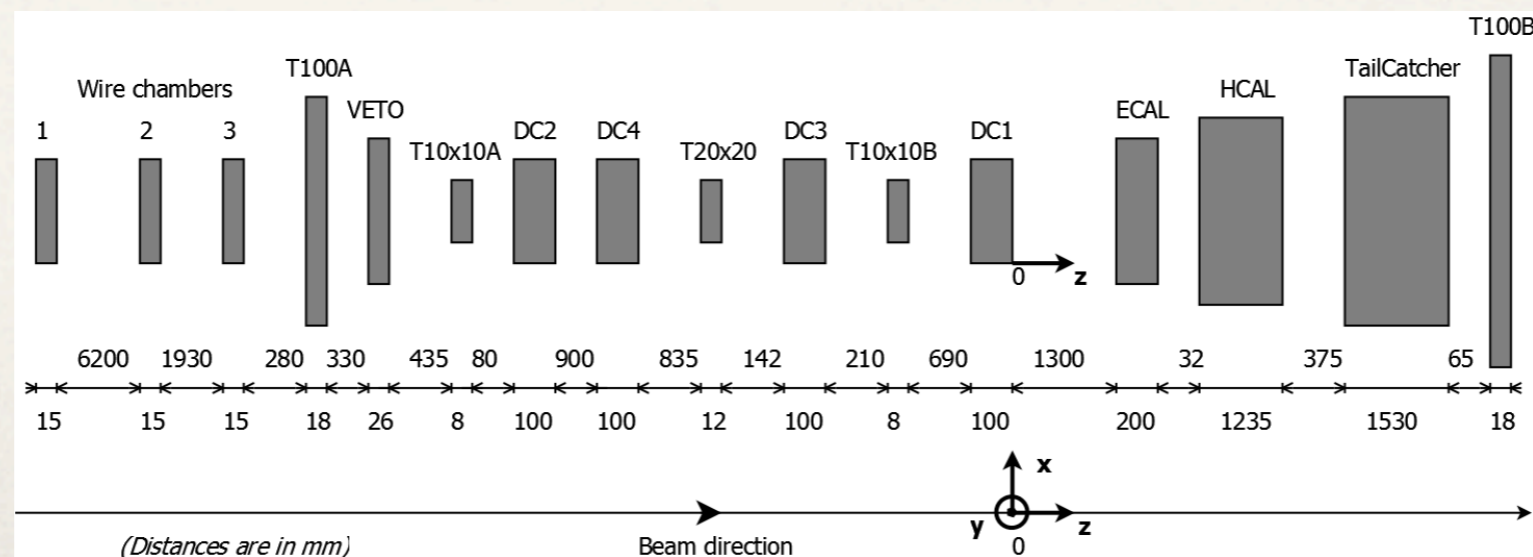
Beam momentum spread:

$2.7 \pm 0.3\%$ for 2-4 GeV

$2.3 \pm 0.3\%$ for 8-32 GeV

Hit energy is measured in MIP units.

The MIP calibration for each channel is performed using 32 GeV muons.

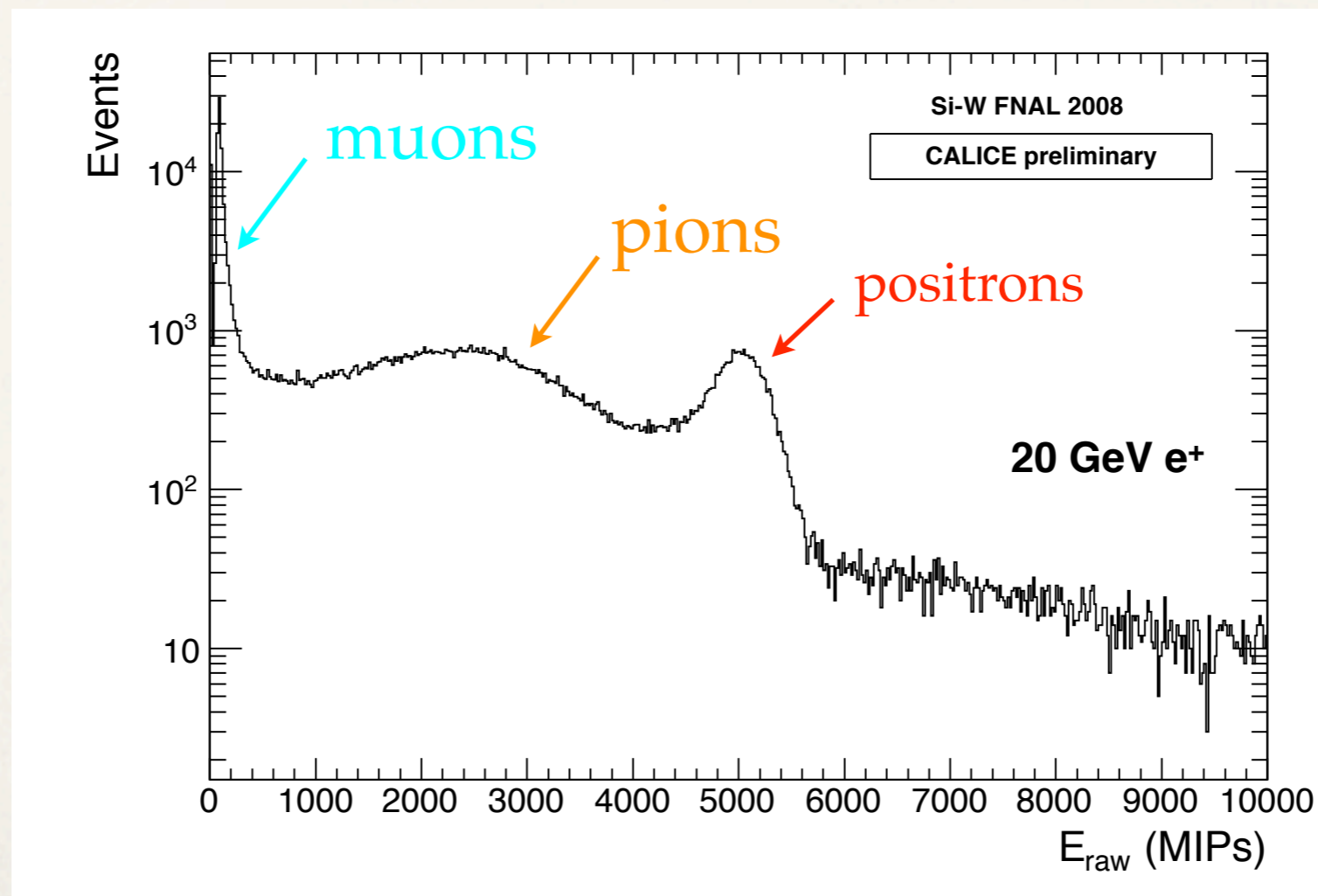


Event Selection

The total energy deposited on ECAL

$$E_{\text{raw}} = \sum_{i=0}^9 E_i + 2 \sum_{i=10}^{19} E_i + 3 \sum_{i=20}^{29} E_i$$

E_i : total energy in i th layer



Event Selection

Event selection

1. set the energy window.

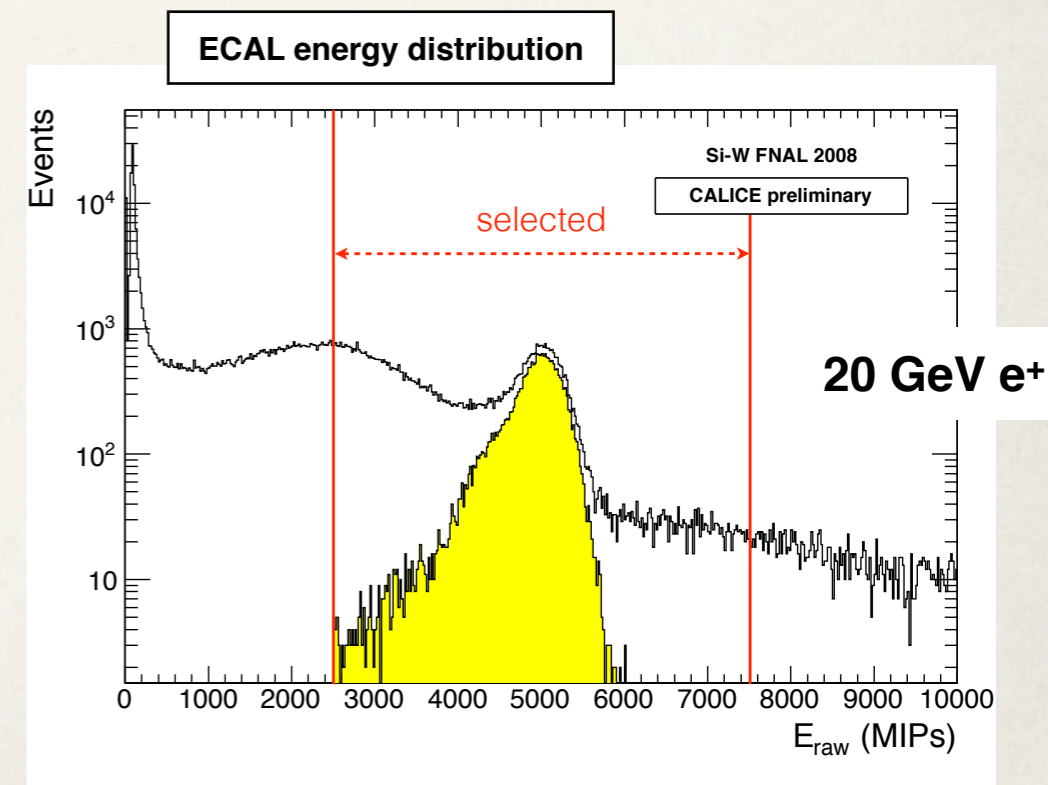
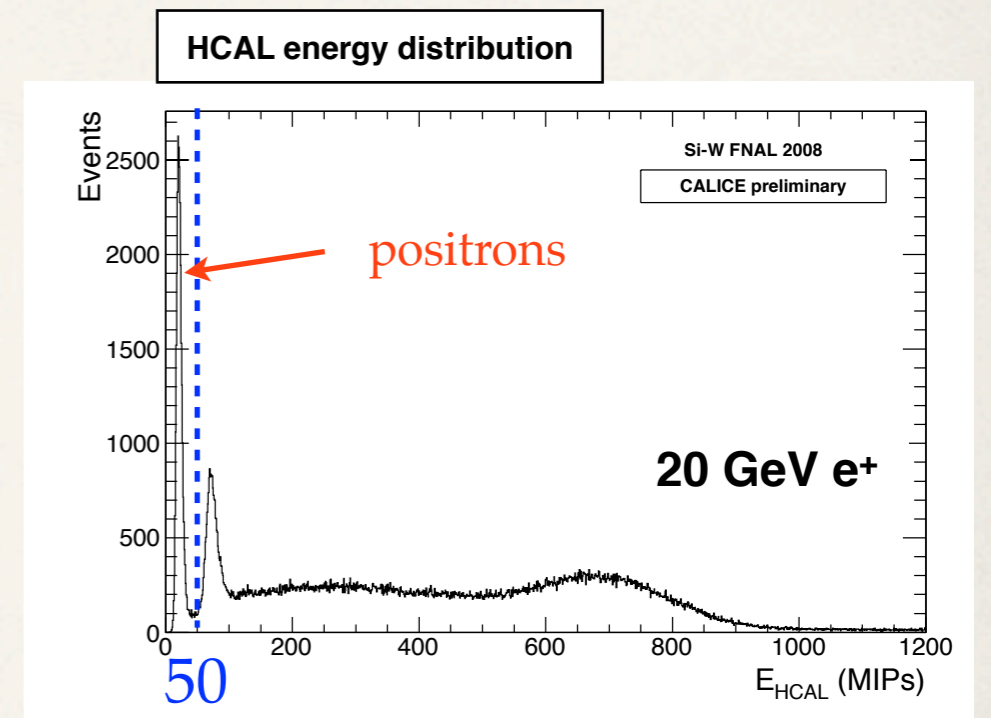
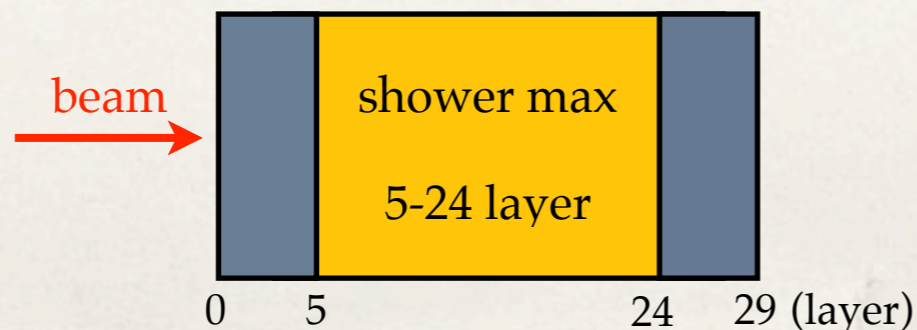
$$125 < \frac{E_{\text{raw}} \text{ (MIPs)}}{E_{\text{beam}} \text{ (GeV)}} < 375$$

2. reject pion contamination by using HCAL information.

$$E_{\text{HCAL}} < 50 \text{ MIPs}$$

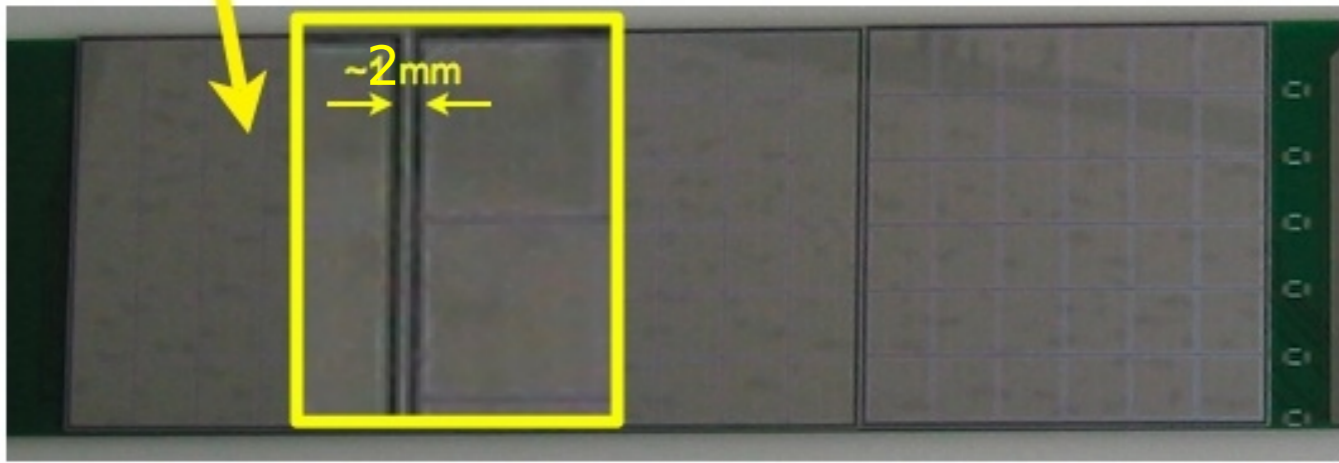
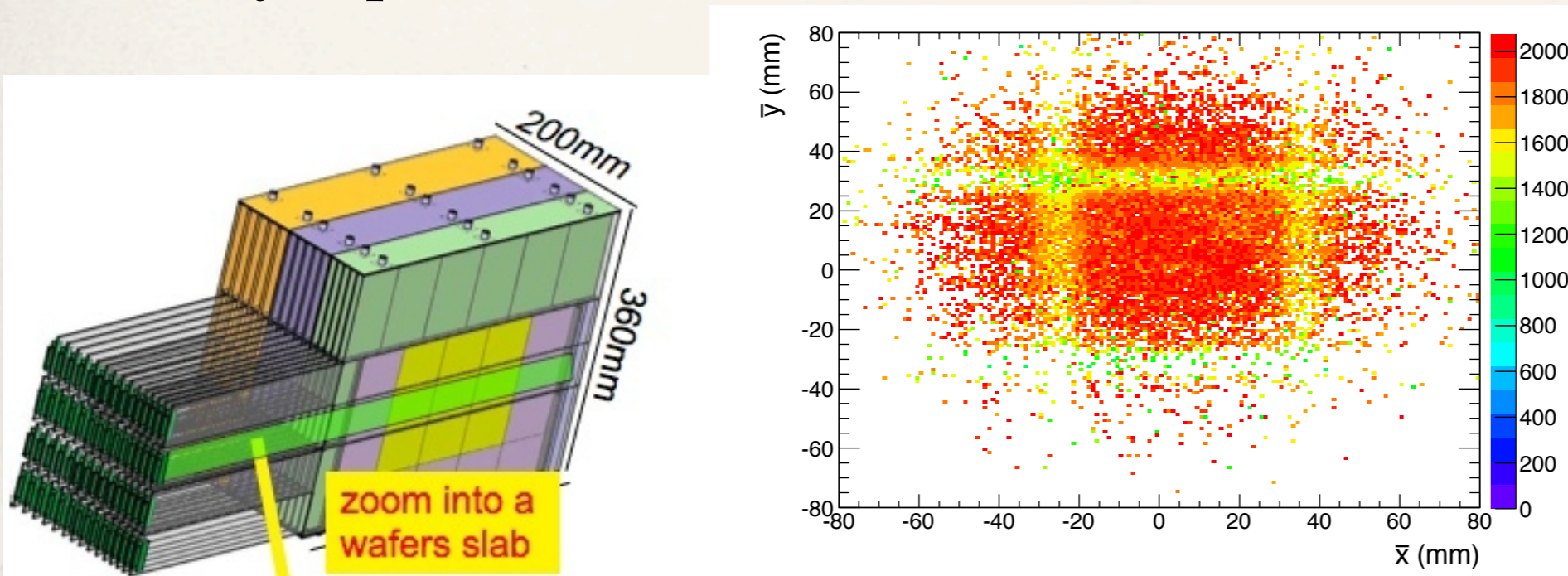
3. reject the event that the shower maximum layer is in the first five layers and the last five layers.

$$5 \leq L_{\text{max}} \leq 24$$



Gap Effect

- ❖ Each silicon wafer has 1 mm guard ring which induces an inactive area.
 - ❖ There are 2 mm inter wafer gaps.
 - ❖ They represents the dominant source of the **non-uniformity**.



E_{mean} (MIPs)

shower barycenter

$$(\bar{x}, \bar{y}) = \left(\frac{\sum_i w E_i x_i}{\sum_i w E_i}, \frac{\sum_i w E_i y_i}{\sum_i w E_i} \right)$$

E_i : hit energy

x_i, y_i : hit position

w : weight (1., 2., 3.)

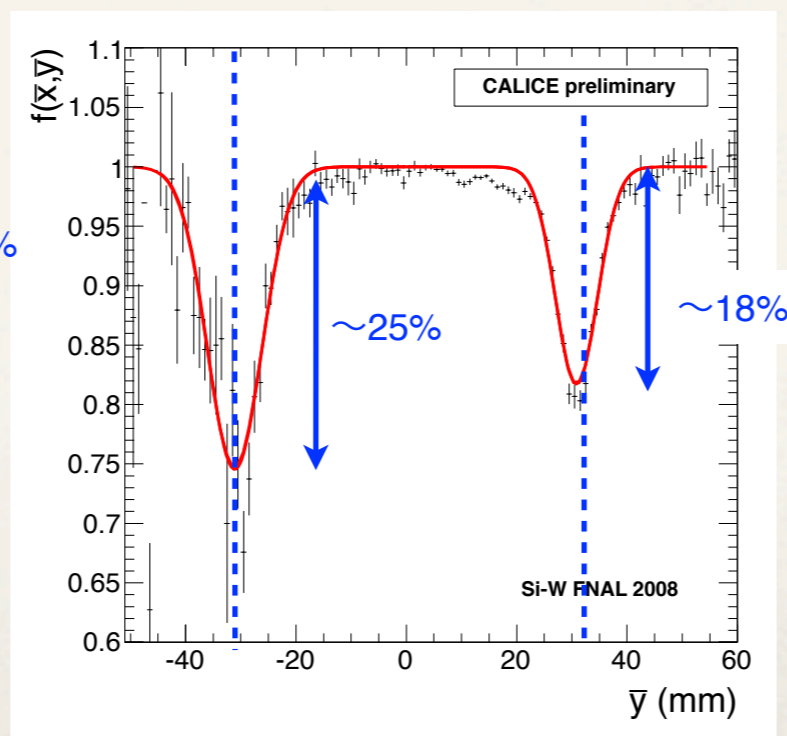
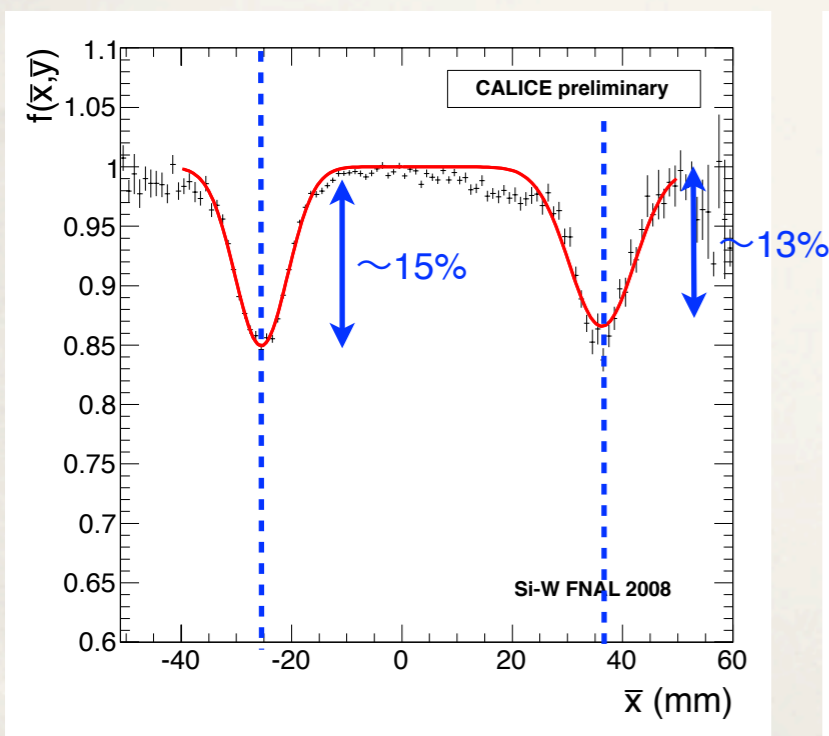
Need to take the gap effect into account in analysis

Gap Correction

- The response around the inter wafer gaps was fitted with the Gaussian.

$$f(\bar{x}, \bar{y}) = \left[1 - a_{x,-} \exp\left\{-\frac{(\bar{x} - x_{-,gap})^2}{2\sigma_{x,-}}\right\}\right] \left[1 - a_{x,+} \exp\left\{-\frac{(\bar{x} - x_{+,gap})^2}{2\sigma_{x,+}}\right\}\right] \\ \times \left[1 - a_{y,-} \exp\left\{-\frac{(\bar{y} - y_{-,gap})^2}{2\sigma_{y,-}}\right\}\right] \left[1 - a_{y,+} \exp\left\{-\frac{(\bar{y} - y_{+,gap})^2}{2\sigma_{y,+}}\right\}\right]$$

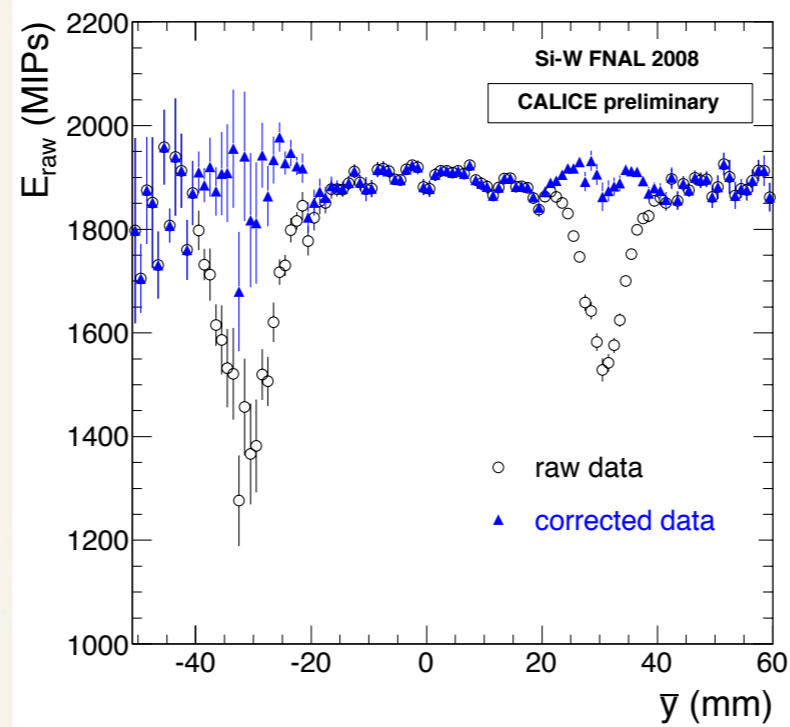
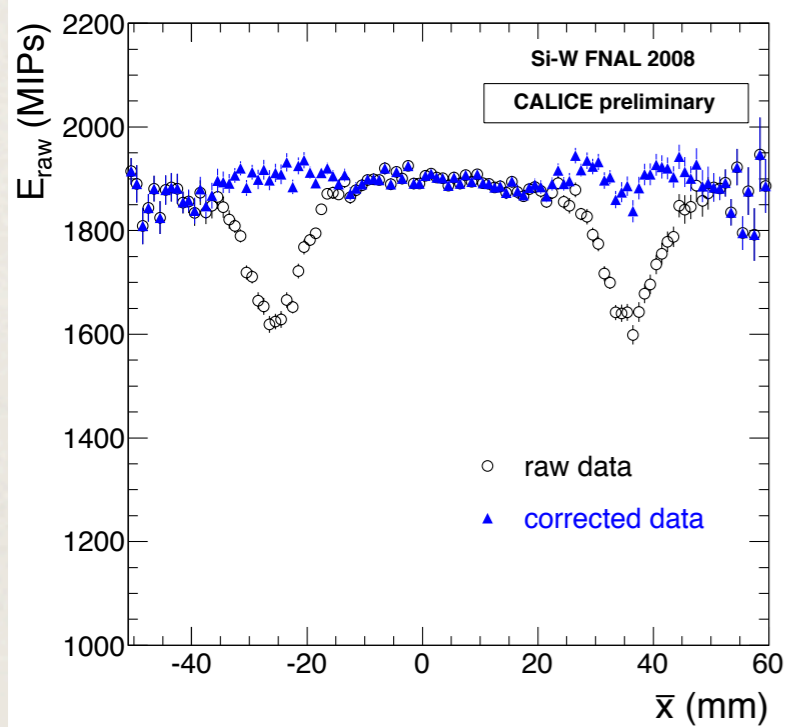
- The value of the parameters $a_{x,\pm}$, $x_{gap,\pm}$, $\sigma_{x,\pm}$, $a_{y,\pm}$, $y_{gap,\pm}$ and $\sigma_{y,\pm}$ was extracted from the results of the fits.



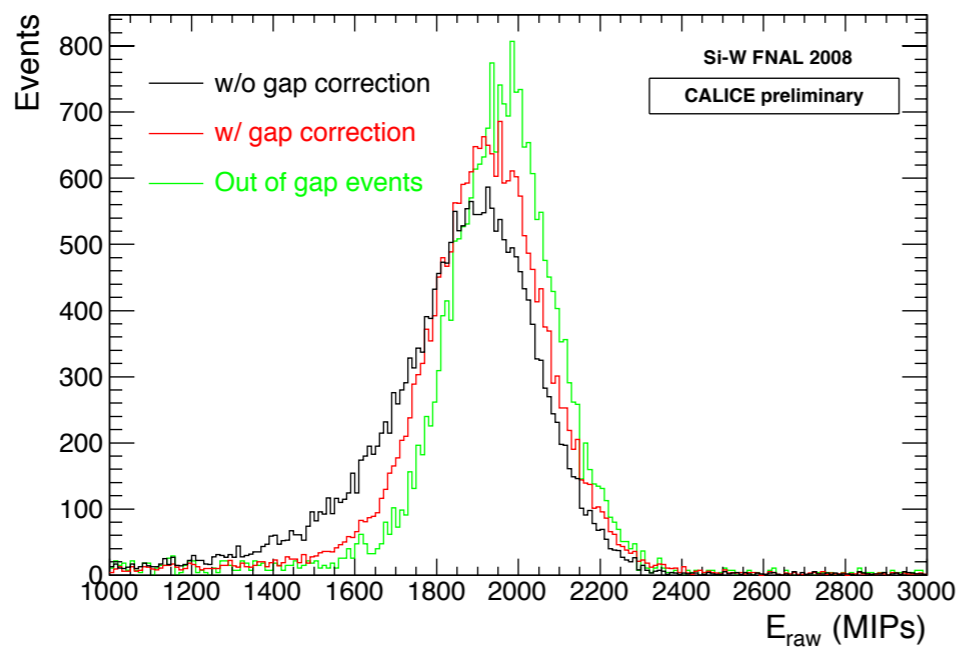
The results of the gaussian fit

	position (mm)	σ (mm)	a
$x_{-,gap}$	-25.5	4.77	0.15
$x_{+,gap}$	36.2	5.92	0.13
$y_{-,gap}$	-31.1	4.94	0.25
$y_{+,gap}$	30.8	3.80	0.18

Gap Correction



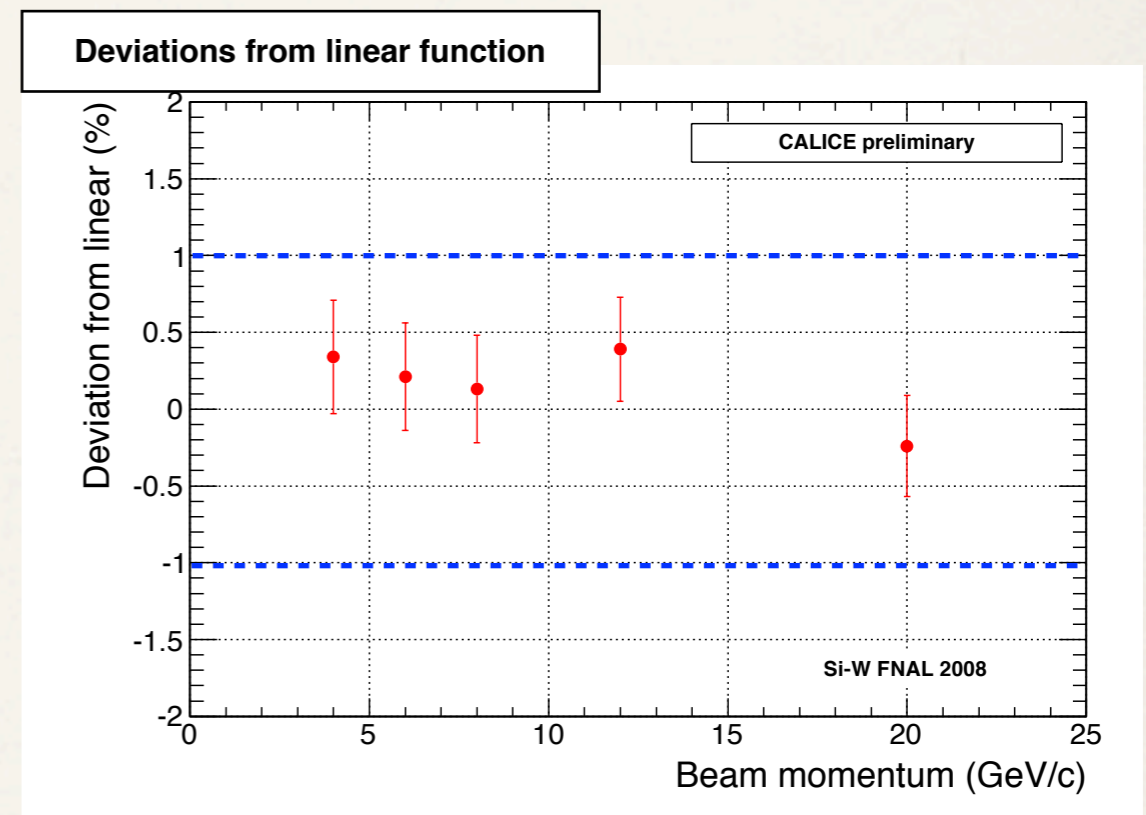
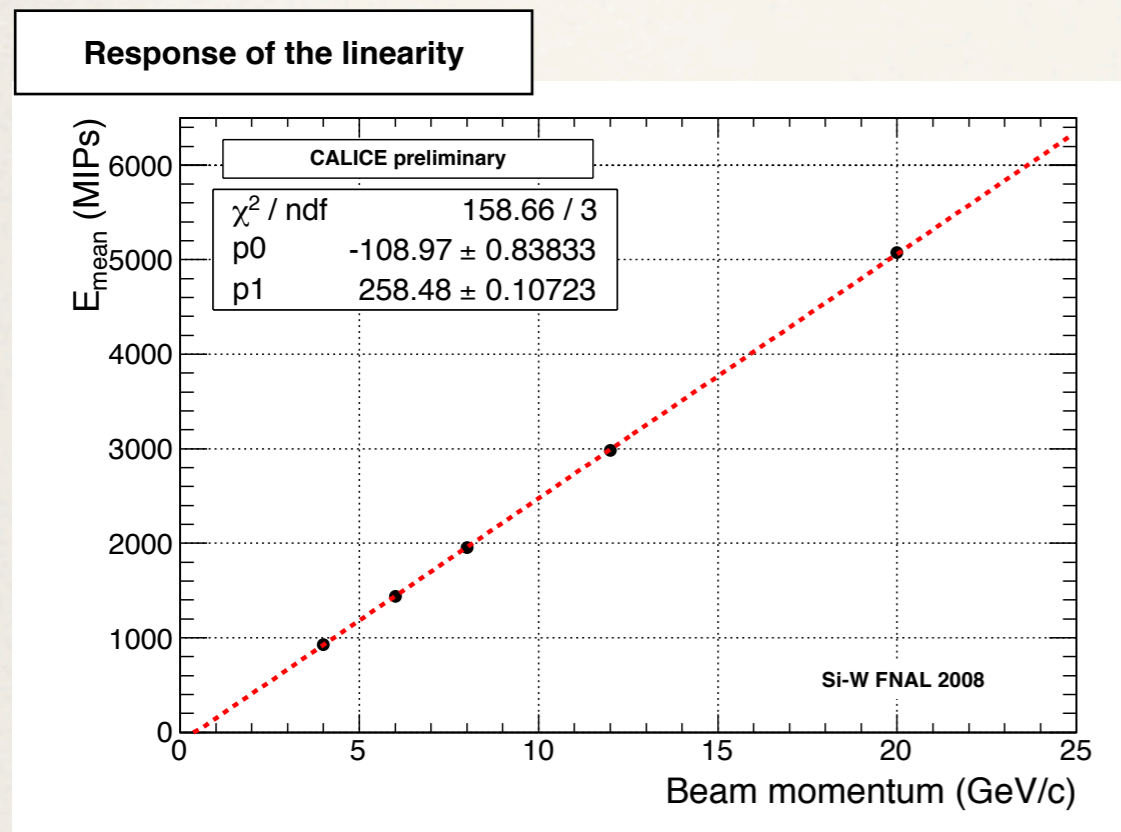
The energy loss in the inter wafer gaps can be corrected by applying $1/f(\bar{x}, \bar{y})$ correction factor.



The shape of the energy distribution becomes more symmetric after gap correction.

Performance (Linearity)

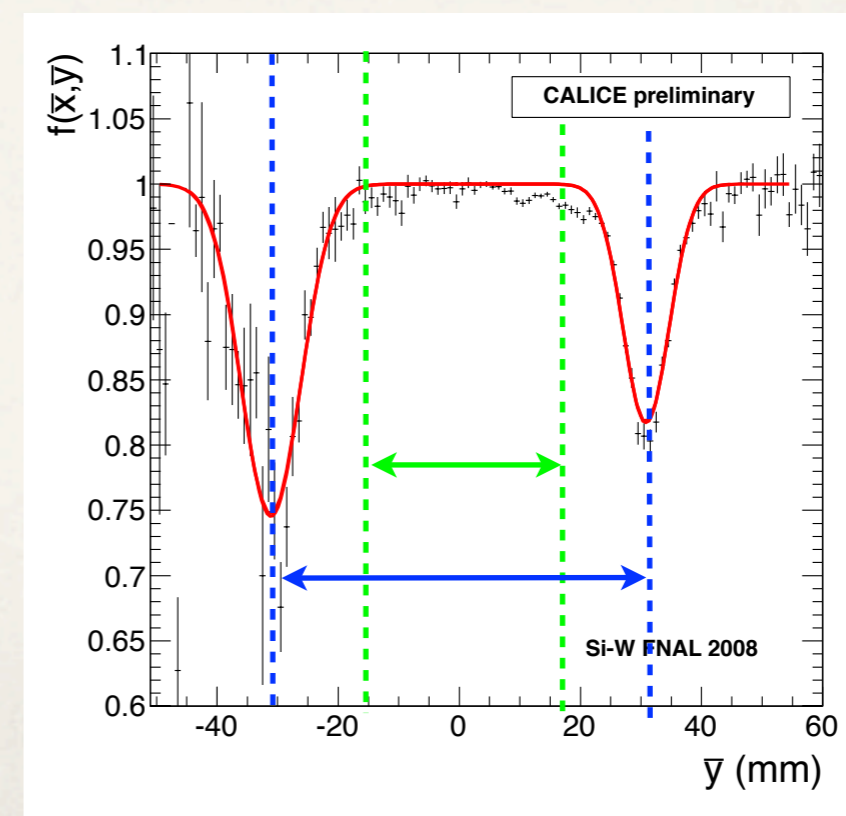
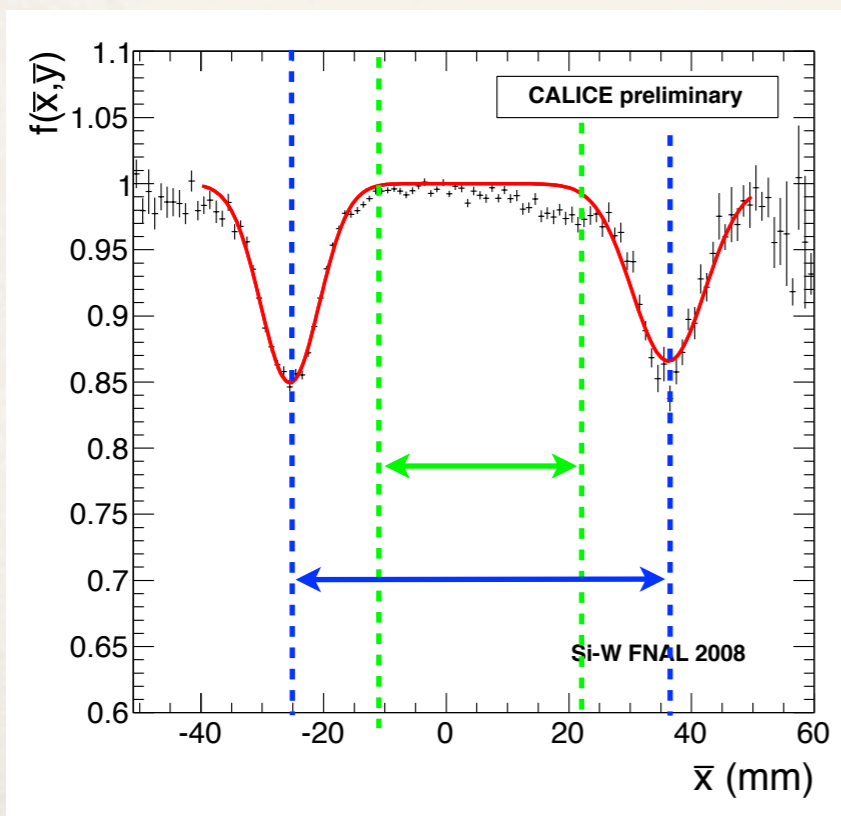
- ❖ We evaluated the performance of linearity and energy resolution after gap correction.



The deviations from linear function are less than 1 %

Performance (Energy resolution)

- ❖ We classified the energy resolution into four situations
 1. “no correction” : the gap correction was not applied for all positron candidates
 2. “gap correction” : the gap correction was applied for all positron candidates
 3. “center region w/ gap” : only positron candidates with the shower barycenter in the central region which includes gaps around the central Si pad are selected.
 4. “center region w/ o gap” : it selects the events in the center region without gap. There is no (little) influence on gap effect



Performance (Energy resolution)

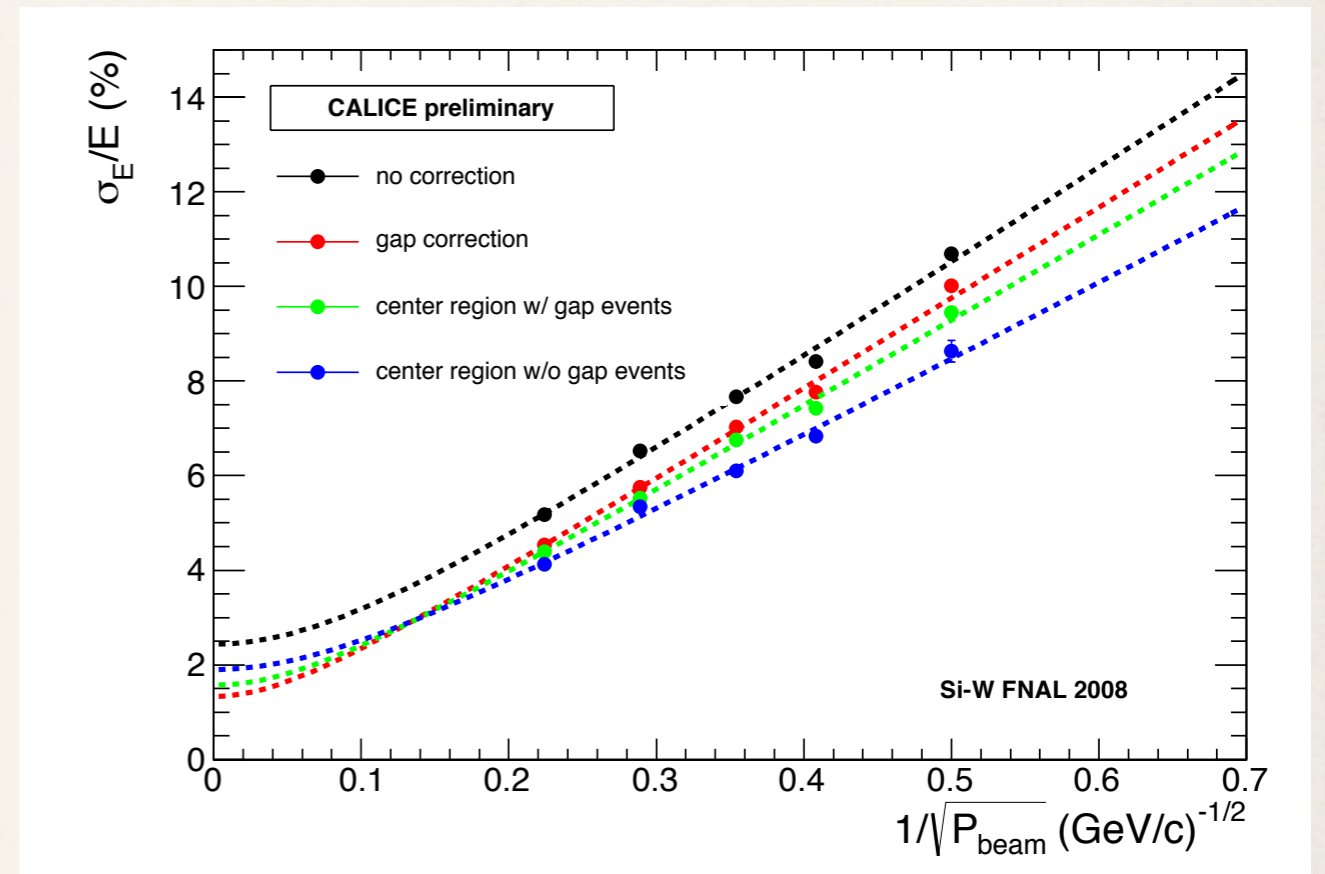
- ❖ We checked the energy resolution in four situations.

Resolution curve:

$$\frac{\sigma_E}{E} = \frac{\sigma_{\text{stoc}}(\%) }{\sqrt{E}} \oplus \sigma_{\text{const}}(\%)$$

The energy resolution of the CERN data was evaluated using center region w/o gap.

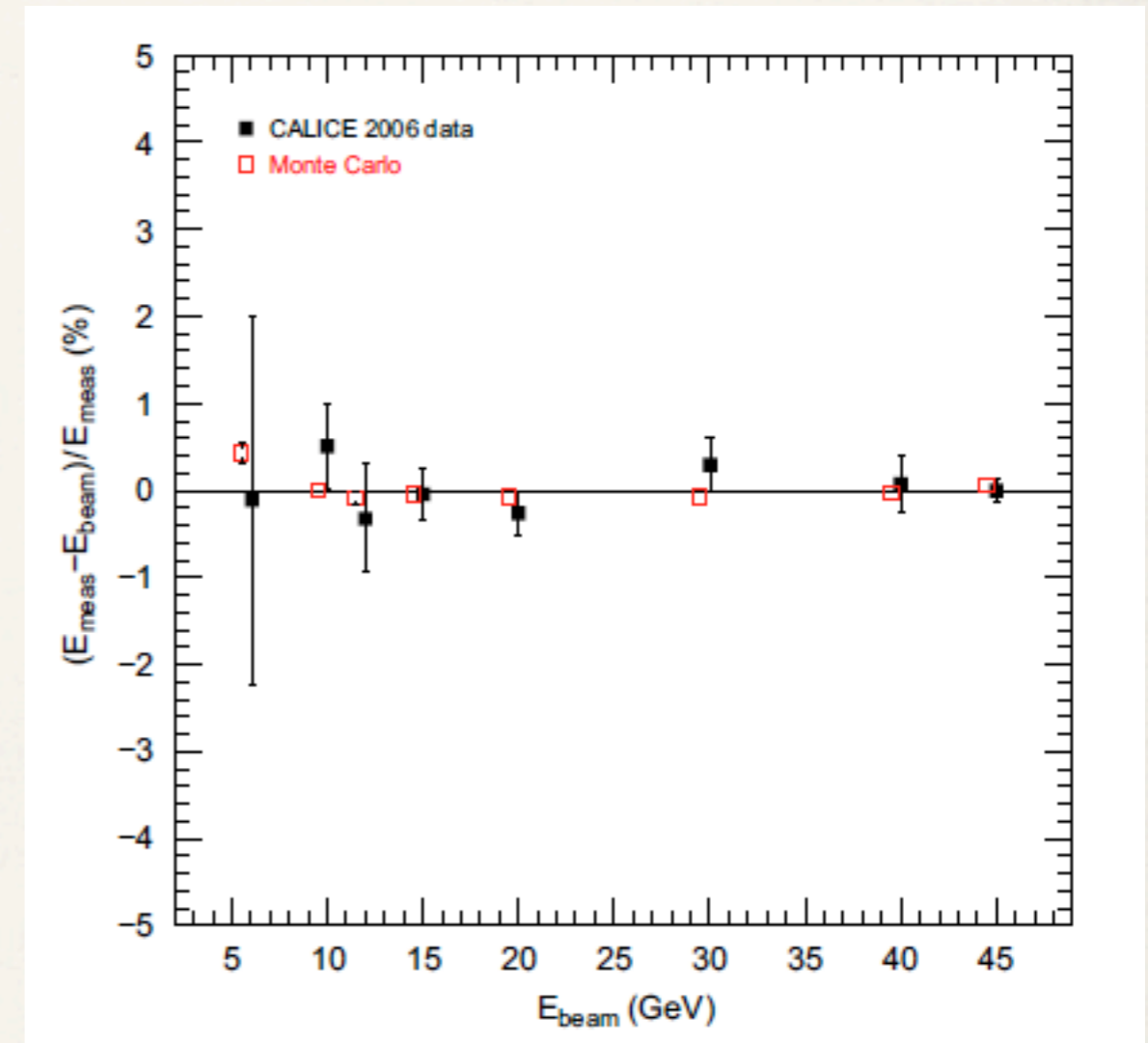
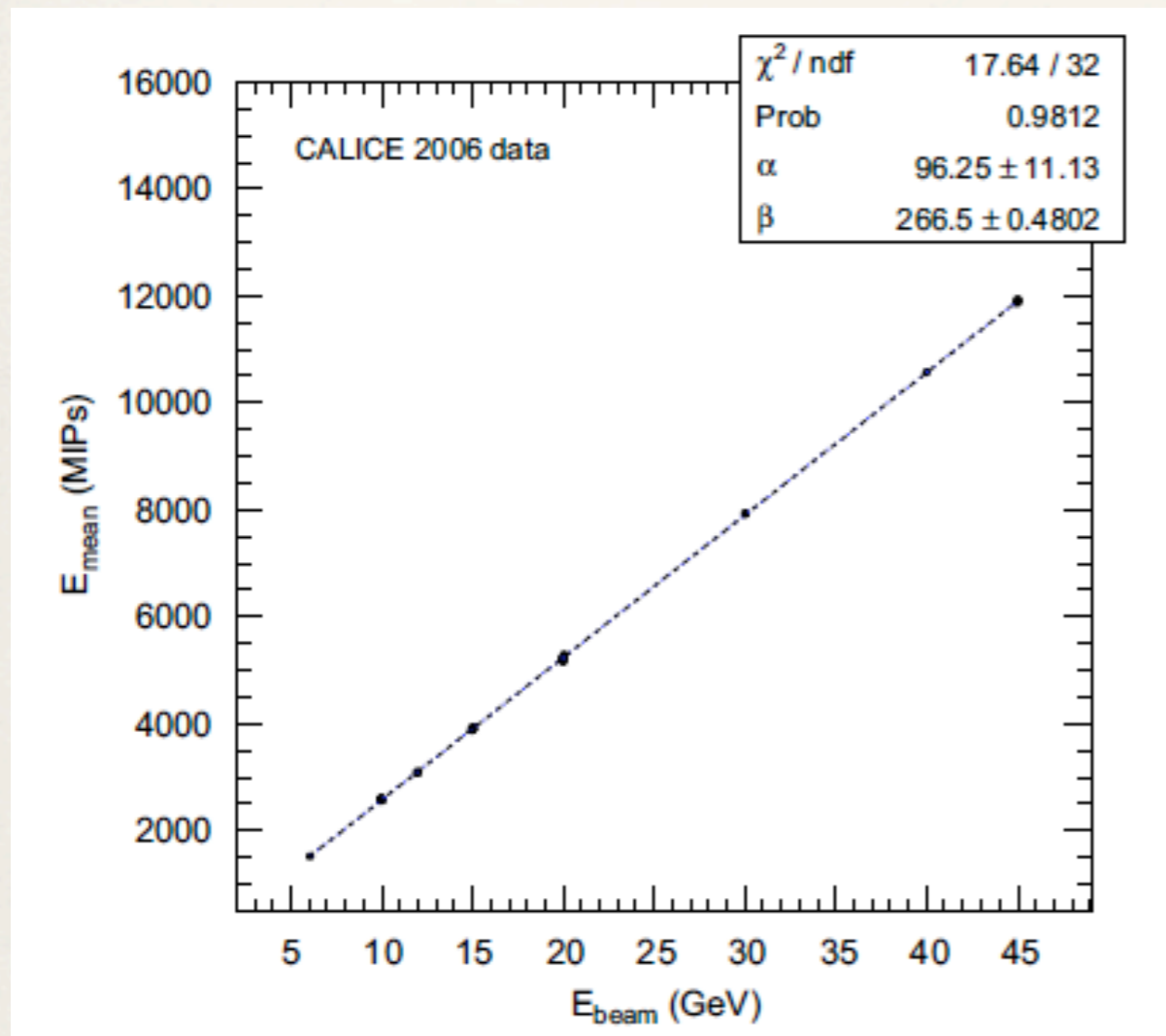
Compared with CERN data, the stochastic term is consistent.



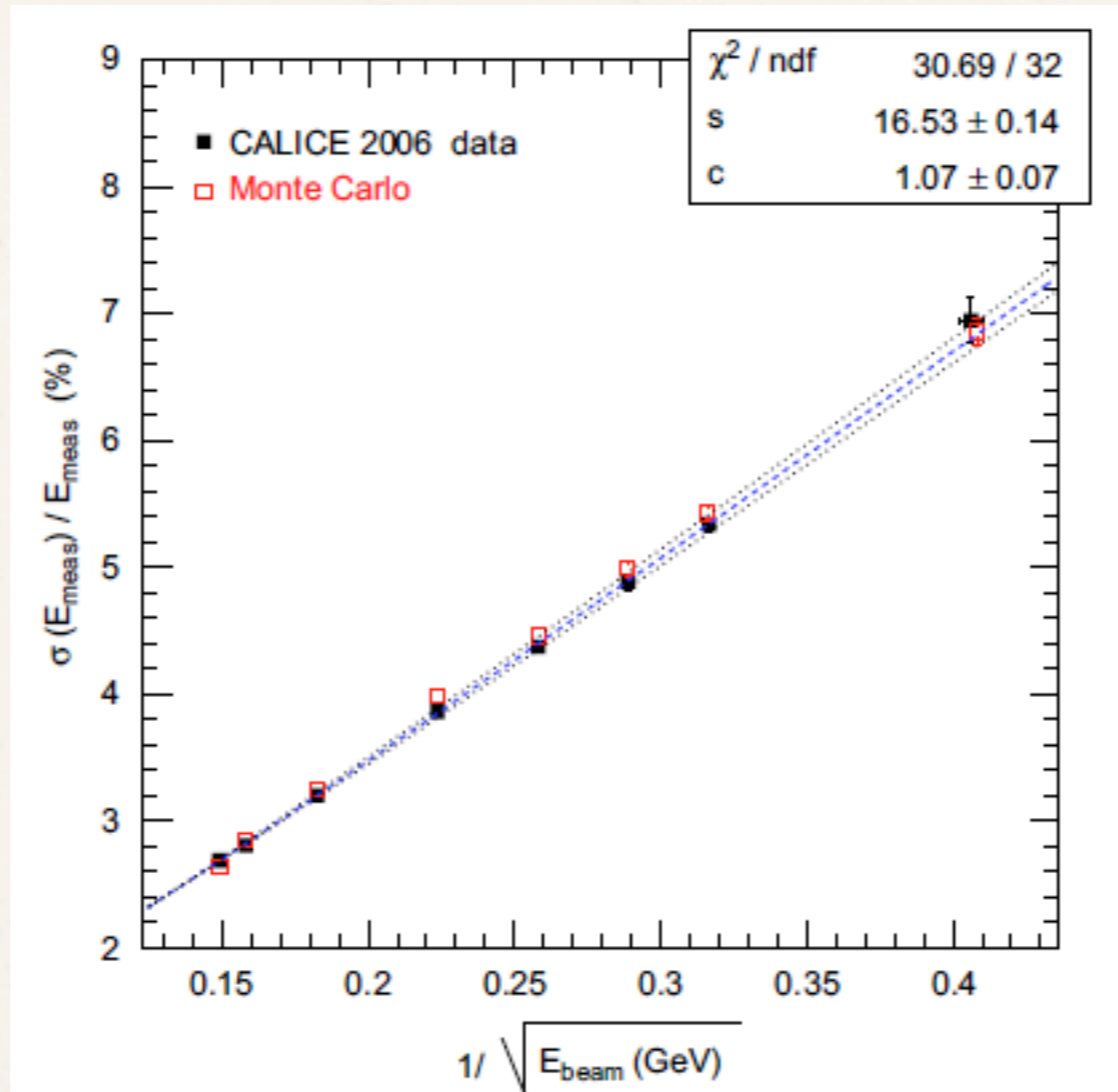
	stochastic	constant
no correction	20.47±0.21%	2.44±0.17%
gap correction	19.33±0.12%	1.33±0.16%
center region w/ gap	18.30±0.16%	1.57±0.15%
center region w/o gap	16.51±0.35%	1.90±0.15%
2006 CERN data	16.53±0.14±0.4%	1.07±0.07±0.1%

The beam momentum spread is not subtracted in the FNAL data

Linearity (CERN 2006)



Energy resolution (CERN 2006)



$$\frac{\sigma(E_{\text{meas}})}{E_{\text{meas}}} = \left(\frac{16.53 \pm 0.14(\text{stat}) \pm 0.4(\text{syst})}{\sqrt{E(\text{GeV})}} \oplus (1.07 \pm 0.07(\text{stat}) \pm 0.1(\text{syst})) \right) \%$$