

# Higgs Recoil Studies

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ILD meeting 2014.9.9

# Outline

- Higgs recoil mass study
  - $\mu\mu h$ ,  $ee h$  @250GeV by S. Watanuki
  - $\mu\mu h$  @350GeV by J. Yan
  - $qqh$  @250GeV by T. Tomita
  - and comparison
- CP-mixture
  - Motivation
  - Current results
- Summary and plan

# Target

One of the advantages of the ILC is **model independent (MI)** analysis of Higgs properties by **recoil method**.

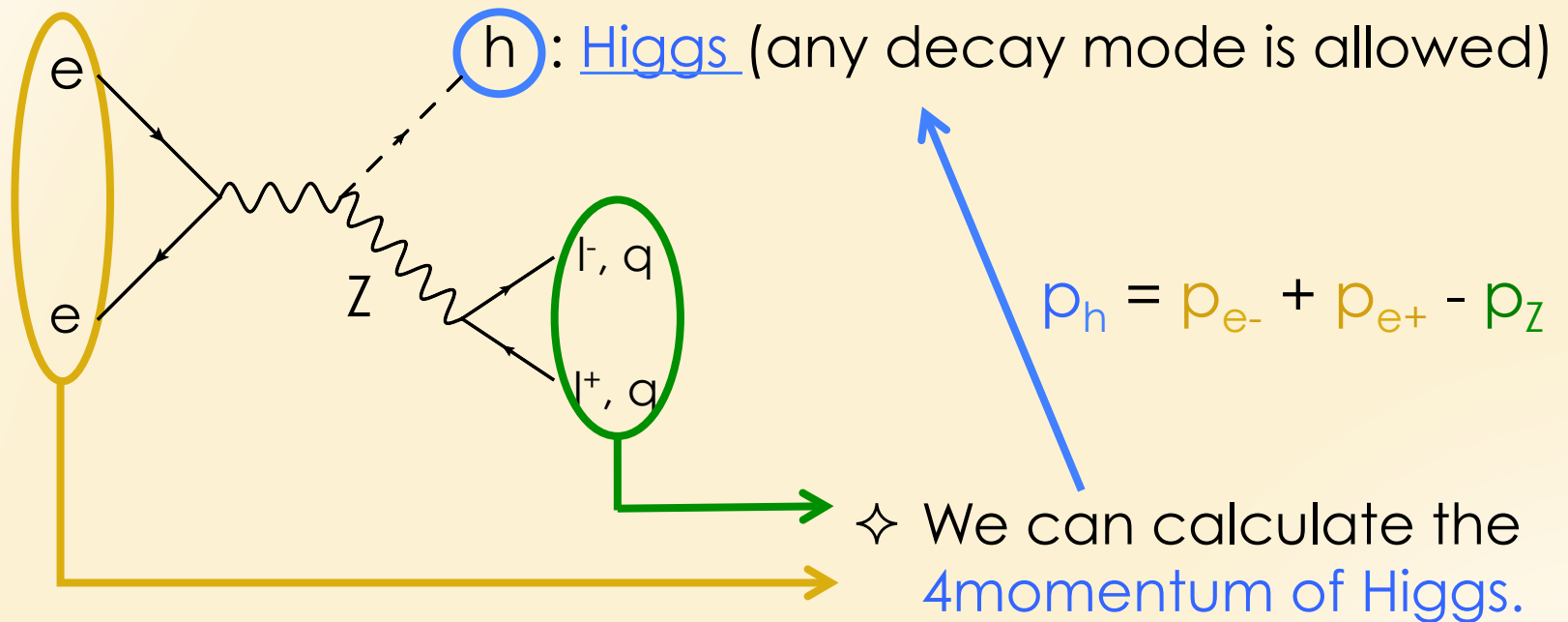


- How precise can we measure Higgs **mass** (only by  $llh$ ) and **cross section** by this method? The considered situations are ...

Production Mode	Higgs mass (GeV)	$E_{CM}$ (GeV)	Integrated Luminosity	Spin Polarization	Detector Simulation
$e^+e^- \rightarrow Zh \rightarrow \mu\mu h, eeh$	125	250	250 $\text{fb}^{-1}$	$P(e^-, e^+) = (\mp 0.8, \pm 0.3)$	ILD_01_v05 (DBD ver.)
$e^+e^- \rightarrow Zh \rightarrow \mu\mu h$	125	350	333 $\text{fb}^{-1}$	$P(e^-, e^+) = (\mp 0.8, \pm 0.3)$	ILD_01_v05 (DBD ver.)
$e^+e^- \rightarrow Zh \rightarrow qqh$	125	250	250 $\text{fb}^{-1}$	$P(e^-, e^+) = (\mp 0.8, \pm 0.3)$	ILD_01_v05 (DBD ver.)

# What's the Recoil Method?

- ILC is a **lepton collider**  
= We already know initial state 4 momentum



Aim for Higgs  $\sigma$  measurement

Directly

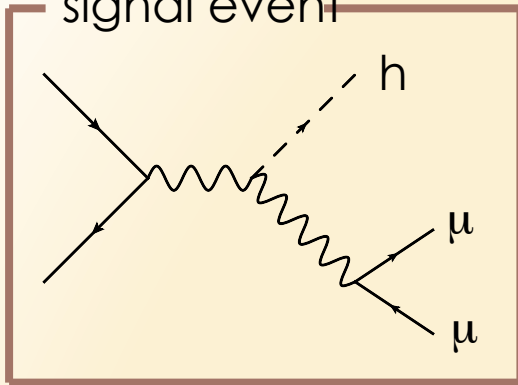
It depends on the model of Higgs decay

Recoil method

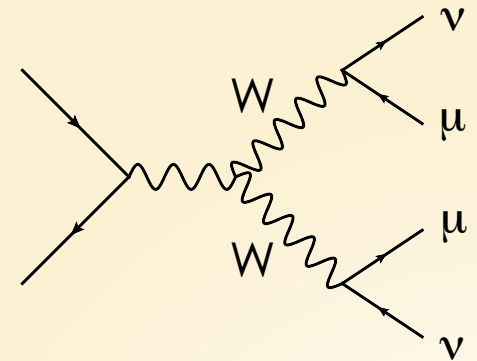
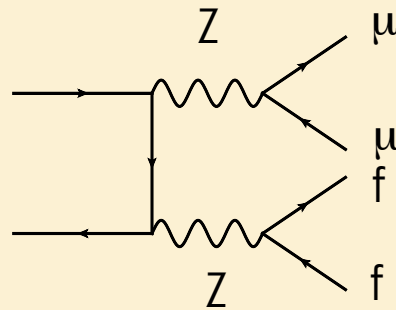
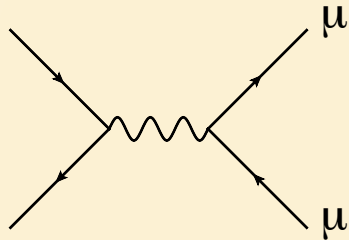
We can measure Higgs **model independently**

# Signal and Background Events

signal event



- These are  $\mu\mu h$  channel signal & BGs.
- For  $eeh$  and  $qqh$  channel study, character of “ $\mu$ ” and “ $\nu$ ” are altered appropriately.



- Dominant Background is “ $\mu\mu$ ”, “ $\mu\mu\nu\nu$ ”, “ $\mu\mu ff$ ” events, and other BG is rejected significantly.

# Lepton Selection

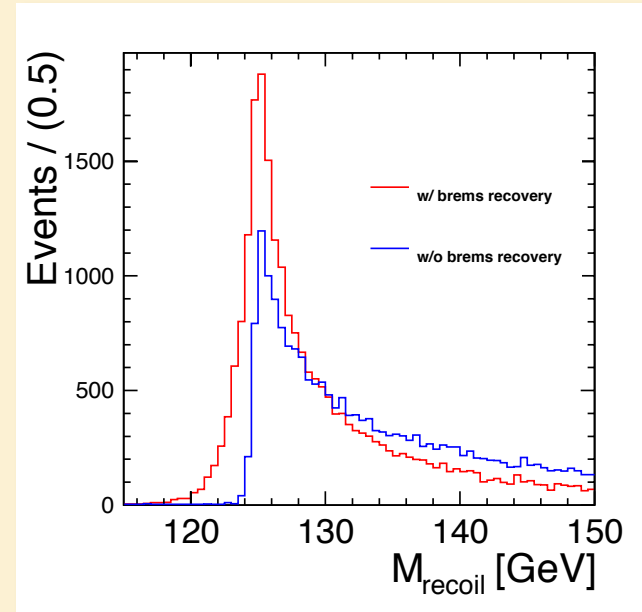
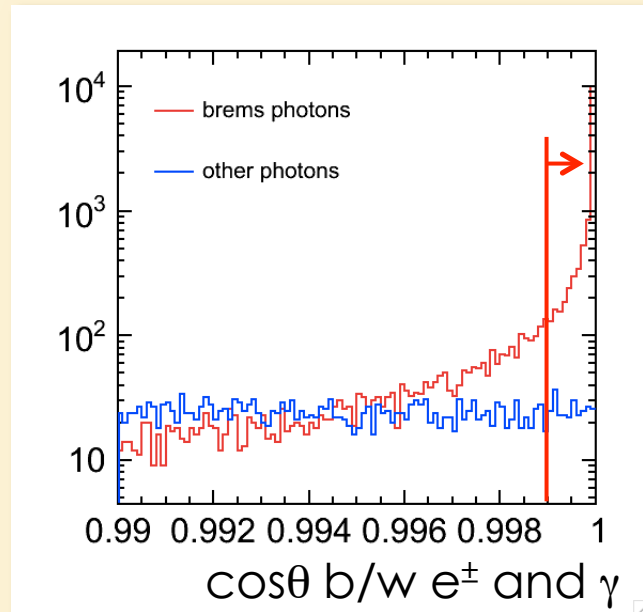
- Muon (electron) selection
  - based on deposited energy on calorimeter
- Good track selection
  - based on error in forward / barrel
- Impact parameter (only for muon)
  - To suppress muons from tau decays

$\mu\mu h, eeh$   
 $@250\text{GeV}$

By S. Watanuki from Tohoku University

# Bremsstrahlung Recovery

- Only for eeh channel, momentum of photon around **final state electron** is added to the electron.
  - $\cos\theta > 0.9995$
  - $\cos\theta > 0.999$  &  $E_{\text{photon}}/E_{\text{electron}} > 0.03$
  - not split photon
- This process contributes to the distribution of recoil mass significantly.



✘ For mass analysis, it is effective not to perform the recovery.



# BG Rejection

$p_{Tdl} > 20 \text{ GeV}$

$M_{dl} \in (80, 100) [\text{GeV}]$

$a_{\text{cop}} \in (0.2, 3.0)$

$\delta p_{Tbal} \in (-10, 10) [\text{GeV}]$

$\cos \theta_{\text{missing}} < 0.99$

$M_{\text{recoil}} \in (115, 150) [\text{GeV}]$

## Likelihood

$\mu\mu$

$\mu\mu\nu\nu$

$\mu\mu$

$\mu\mu\gamma$

$\mu\mu\gamma$

$\mu\mu$   
 $\mu\mu\nu\nu$   
 $\mu\mu ff$

$\mu\mu$   
 $\mu\mu\nu\nu$   
 $\mu\mu ff$

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$\mu\mu$

$\mu\mu\nu\nu$

ed

$\mu\mu h$	signal	ll	llvv	llff	others
No Cut	2603	3.2M	507166	390041	7.1M
After Cut	1386	322	1479	1054	3
eeh	signal	ll	llvv	llff	others
No Cut	2729	7.8M	520624	404279	2.5M
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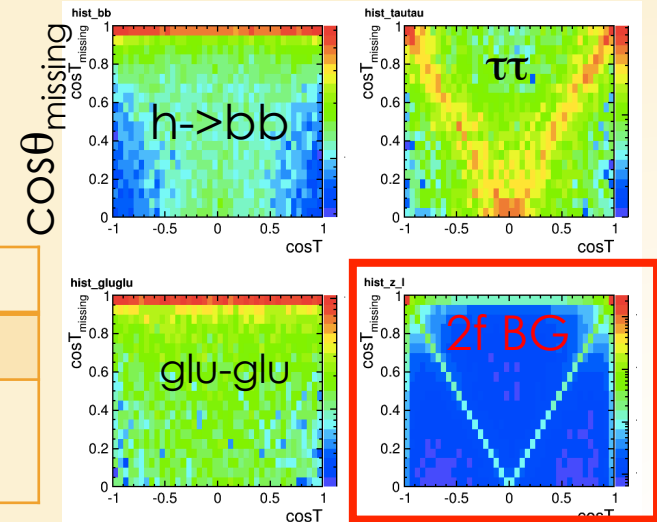
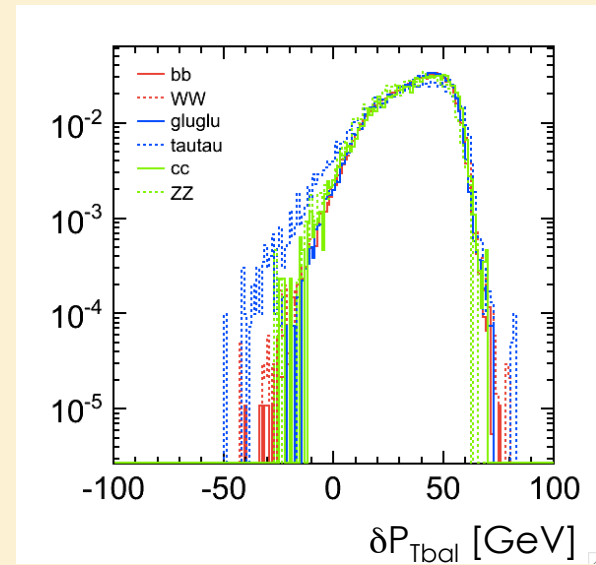
$\mu\mu h$

$\mu\mu\nu\nu$

$\mu\mu ff$

# Unbiased Selection

- $\delta P_{Tbal}$  and  $\cos\theta_{missing}$  cut has bias for Higgs decay modes.
- To avoid this bias problem, some additional conditions are needed
- $\delta P_{Tbal} = P_{Tdl} - P_{Tphoton}$ 
  - photon should satisfy ...
    - $m_{2\gamma} > 0.2$  [GeV]
    - or  $E_{\gamma} > 60$  [GeV]
- $\cos\theta_{missing}$  :  $\cos\theta$  of all PFOs
  - $|\cos\theta_{missing}| < 0.99$
  - or  $|\cos\theta_{Z\ boson}| < 0.8$
- These additional condition **avoid bias**, but efficiency of **BG rejection is sacrificed**.



	bb	glu-glu	$\tau\tau$	BG (II)
$\cos\theta_{miss} < 0.99$	95.1%	92.8%	99.2%	41.1%
$\cos\theta_{miss} < 0.99$ or $ \cos\theta  < 0.8$	99.3%	99.1%	99.8%	74.6%

$\cos\theta_{Z\ boson}$

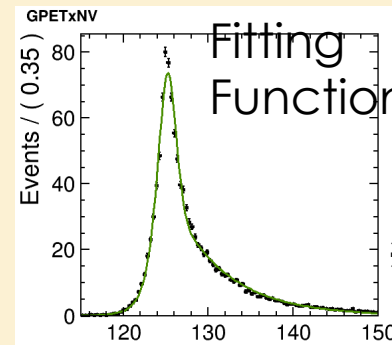
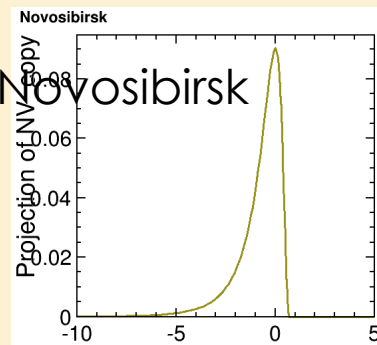
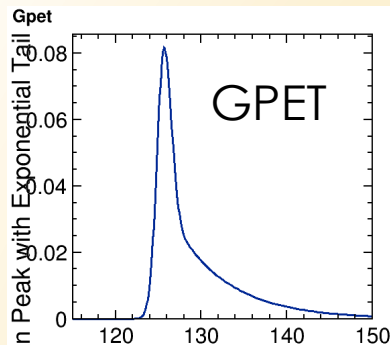
# Signal Efficiency

- After that, bias of signal efficiency for Higgs decay is eliminated.

<b>H decay mode</b>	<b><math>\mu\mu h</math> efficiency [%]</b>	<b>eeh efficiency [%]</b>
bb	55.61	45.62
WW	55.39	44.95
gluglu	55.16	45.02
$\tau\tau$	55.42	44.49
cc	55.60	45.14
ZZ	54.04	45.51

- Systematic error due to efficiency in decay modes is 3%.
- (If we could use the information on measured cross section for higgs decay modes, the error should be much smaller)

# Fitting Function



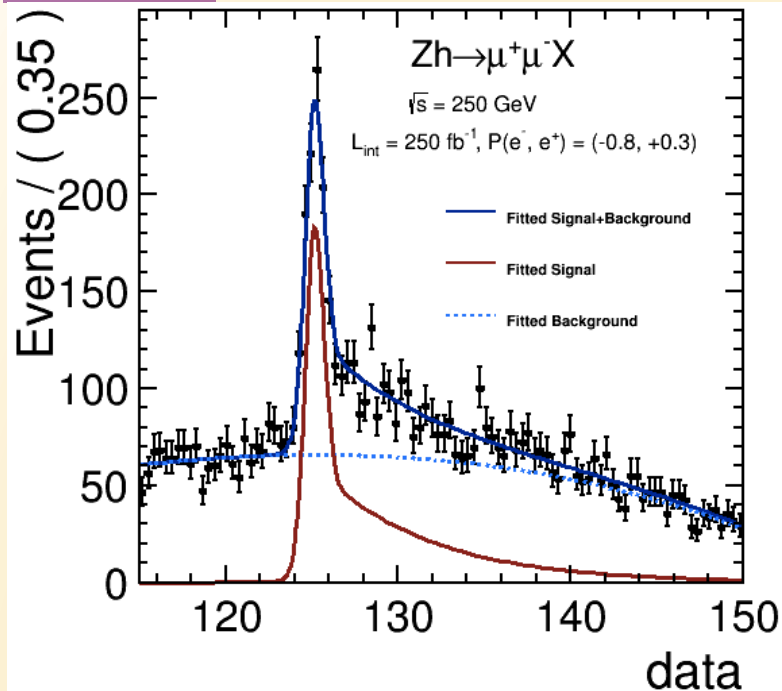
- GPET is constructed by Gaussian peak and exponential tail.
- Novosibirsk can express uncertainty of lepton detection.
  - For detail of Novosibirsk function, please check [Nuclear Instruments and Methods in Physics Research A 441 (2000) 401-426]
- For BG fitting, 3<sup>rd</sup> order polynomial is used. (BG shape is determined separately from signal shape determination)

	GPET (signal)					3 <sup>rd</sup> order poly. (BG)			Yields	
	mean	width	k	b	NV	p1	p2	p3	Y <sub>sig</sub>	Y <sub>BG</sub>
Fitting	float	float	float	float	float	float	float	float	float	float
toyMC	float	fix	fix	fix	fix	fix	fix	fix	float	float

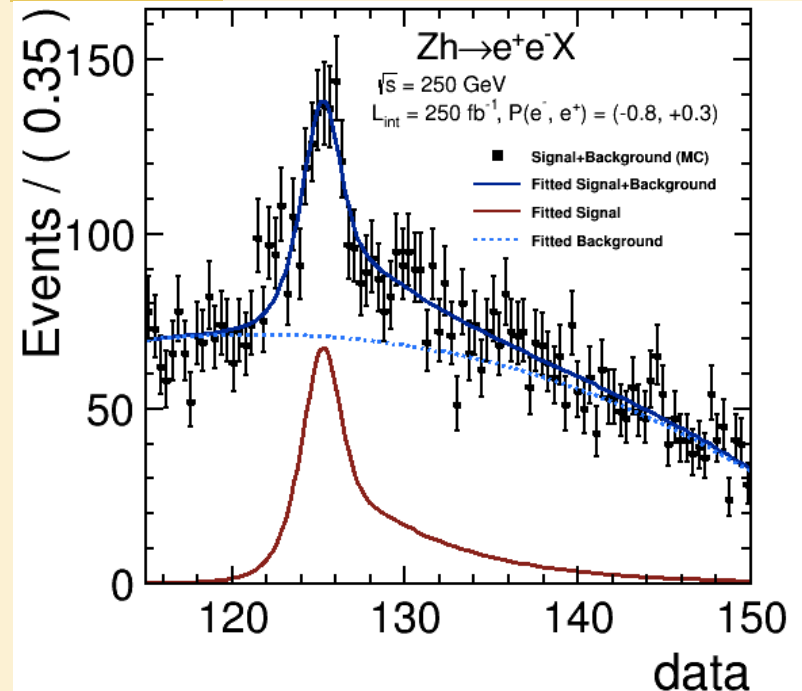
⊗ k : boundary, b : junction

# Fitting Results

$\mu\mu h$



$eeh$

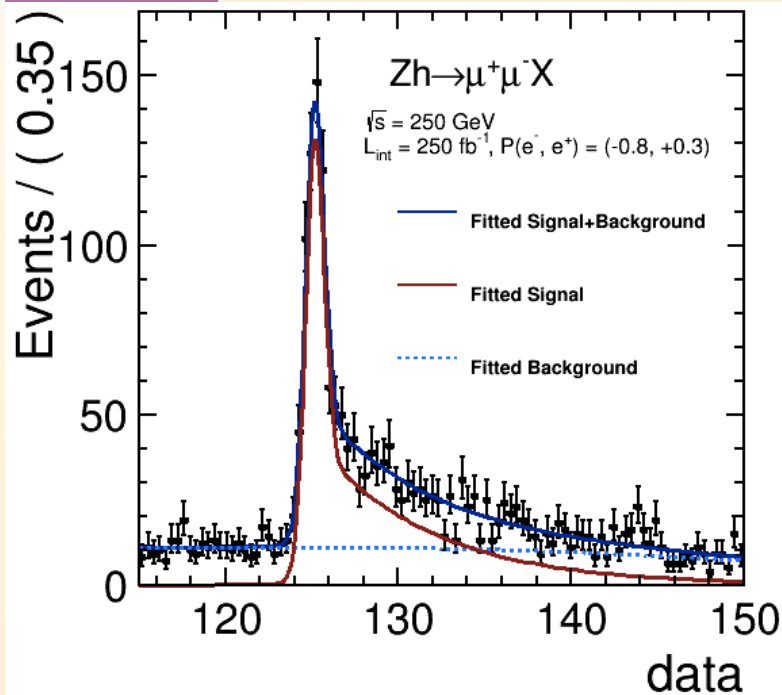


$L=250\text{fb}^{-1}$ $P(e^-, e^+) = (-0.8, +0.3)$	$\mu\mu h$		$eeh$		combined	
$\Delta\sigma/\sigma$	4.2%	3.8%	6.0%	5.6%	3.4%	3.1%
$\Delta\text{mass [MeV]}$	34	33	231	89	34	31

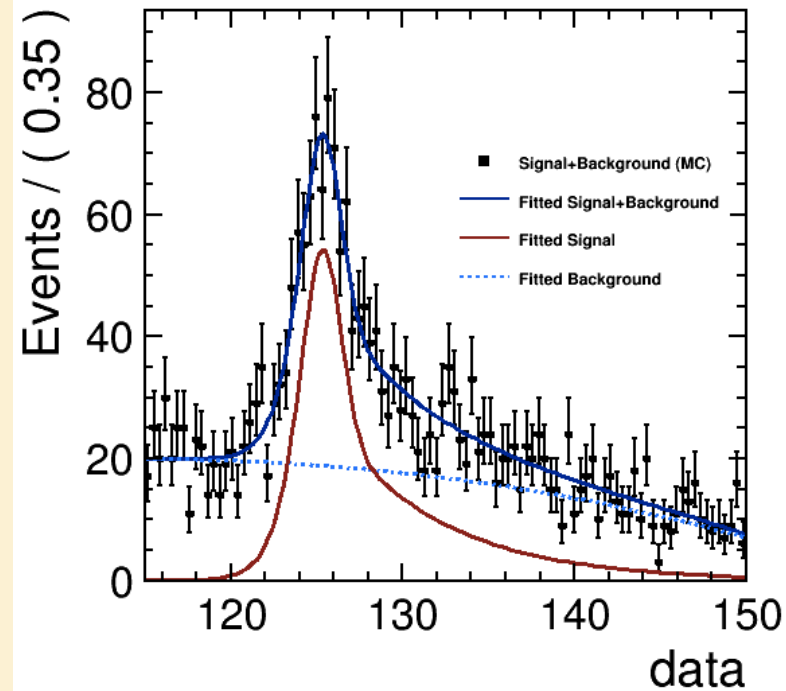
✘ Red value means semi-MI analysis in which visible energy cut is performed. 14

# Fitting Results (Right Handed)

$\mu\mu h$

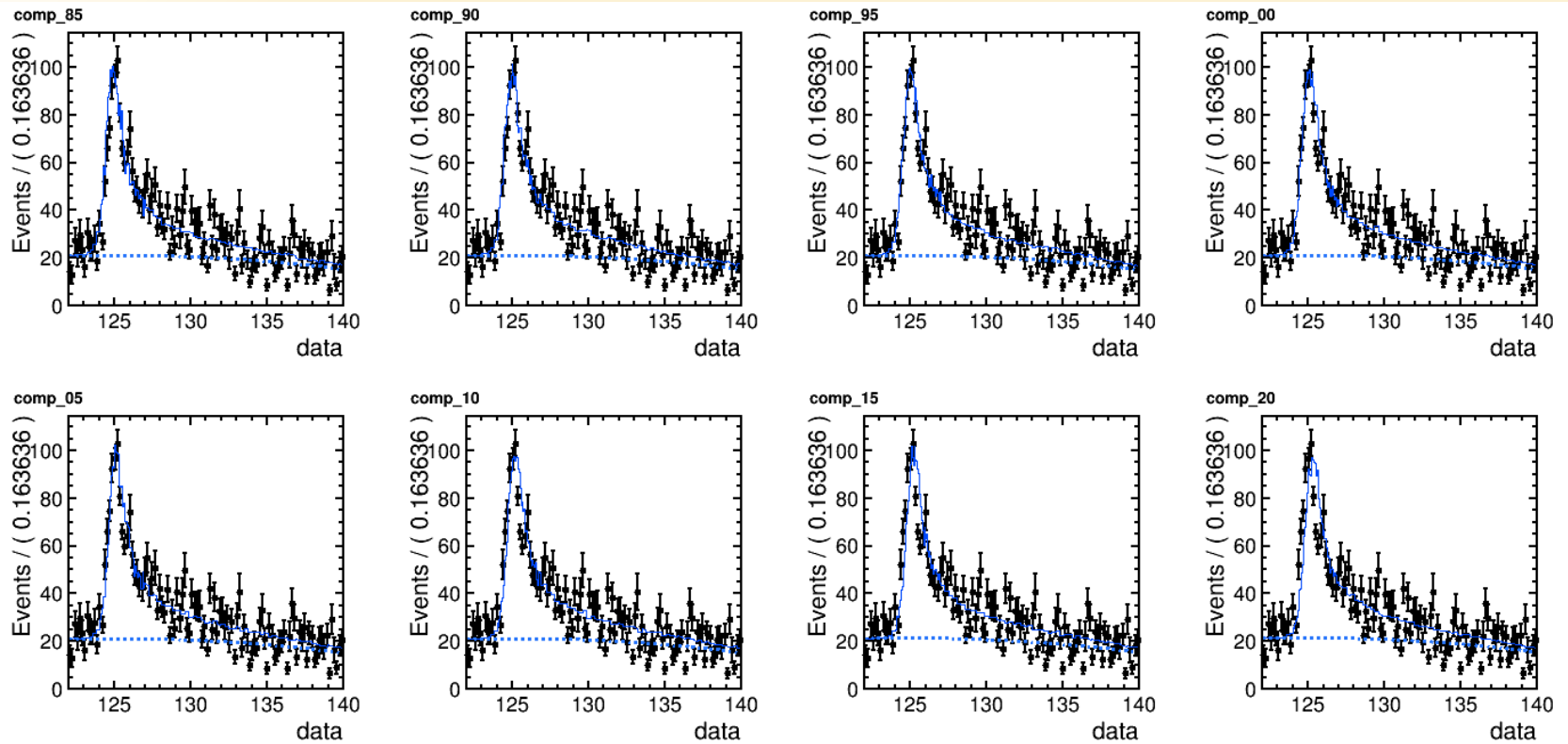


$ee h$



$L=250\text{fb}^{-1}$ $P(e^-, e^+) = (-0.8, +0.3)$	$\mu\mu h$	$ee h$	combined
$\Delta\sigma/\sigma$	3.8%	6.0%	3.2%
$\Delta\text{mass [MeV]}$	31	214	31

# Mass Template Method



- For mass measurement, template method is also tried.
- Non-uniform binned histogram is used as PDF to fit.

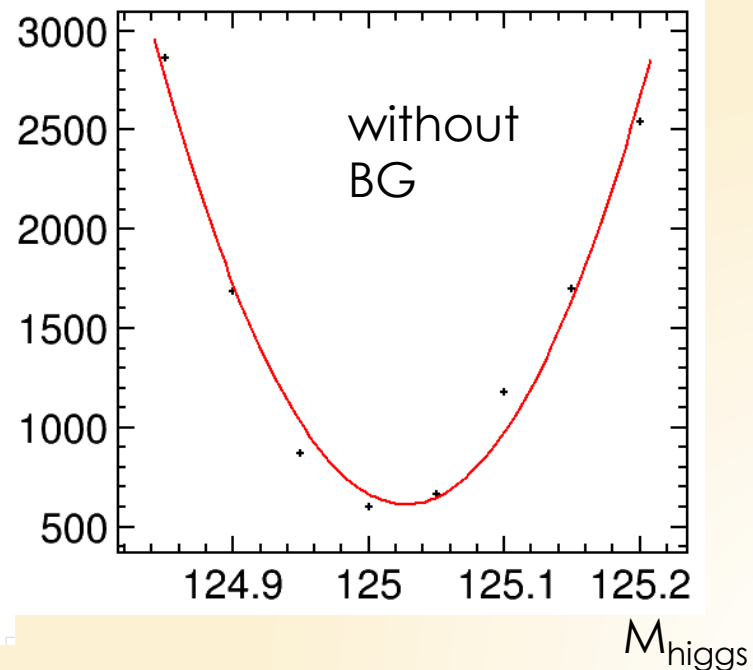
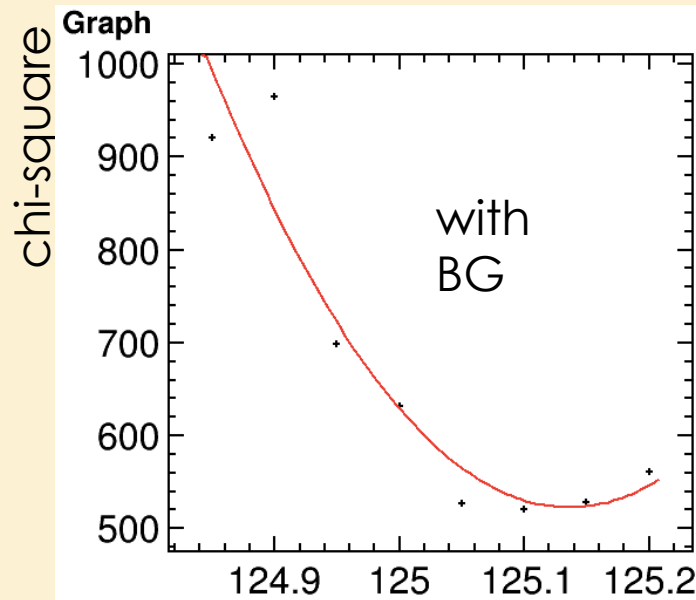
region [GeV]	[122, 124]	[124, 127]	[127, 140]
# of bins	10	50	50

- BG PDF is used fitted 3<sup>rd</sup> order polynomial.



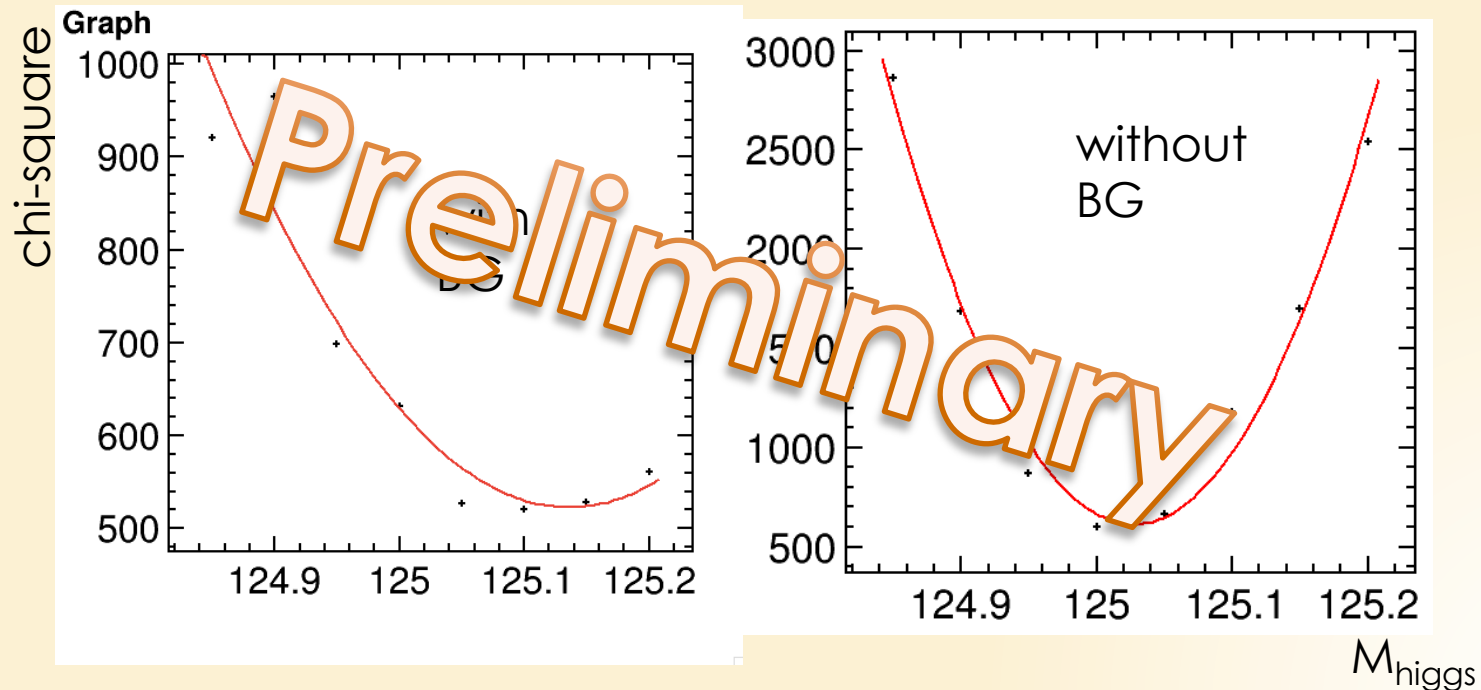
# Chi-square Plot

- Chi2 of any fitting is plotted, and fitted by parabola.
- Minimum point :
  - $x = 125.136 \pm 0.013$  [GeV]
  - $x = 125.027 \pm 0.003$  [GeV] (w/o BG)



# Chi-square Plot

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# Next Plan

- Further investigation of mass template method is needed.
- Estimate sensitivity to Higgs CP-mixture, which is from anomalous coupling in 2HDM, by Z production angle.

$\mu\mu h$   
@350GeV

By J. Yan from University of Tokyo

# Status

- Goal :
  - Precise measurement of Higgs cross section
  - Contribute to the decision for ILC run scenario
- BG : included all **2f, 4f, 6f** processes
- Full ILD detector simulation
- Compare results between  $P(-0.8, +0.3)$  and  $P(+0.8, -0.3)$ , between 350GeV and 250GeV
- Final selection for  $E_{cm} = 350\text{GeV}$ 
  - $84 < M_{inv} < 98$  (GeV)
  - $10 < P_{Tdl} < 140$  (GeV)
  - $dPT_{bal} = |P_{Tdl} - PT_{\gamma_{max}}| > 10$  (GeV)
  - coplanarity  $< 3$
  - $|\cos\theta_{Zpro}| < 0.91$
- $120 < M_{recoil} < 140$  (GeV)

# Cut Efficiency

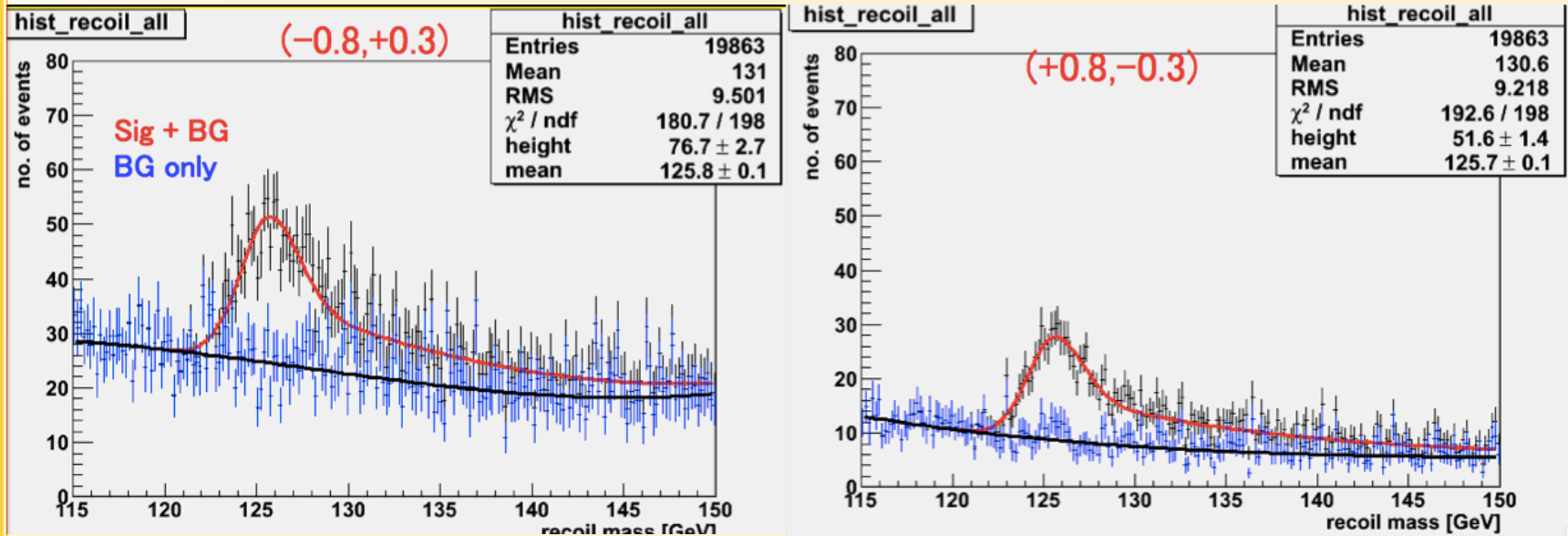
	signal	BG	2f_Z_l	4f_WW_sl	4f_ZZ_sl
raw events	2288	32M	2M	2.7M	188087
best m pair	2254	2M	946129	236802	42345
$D_0$	2241	1.8M	925330	152599	39825
track angle	2205	1.6M	843738	136568	36073
$M_{inv}$	1826	313998	269446	5702	16365
$P_{Tdl}$	1819	111823	71877	5659	14934
$\delta P_{Tbal}$	1798	48694	10674	5505	14108
acop	1773	44735	9612	4578	13347
$\cos\theta_z$	1698	30428	5709	2940	9147
$M_{recoil}$	1088	2700	276	405	1123

- After selection
  - signal efficiency = 47.6 +/- 0.5%
  - S/B = 0.40, significance = 17.2

# Fitting

- Signal is fitted by GPET
- BG is fitted by 3<sup>rd</sup> order polynomial
- Float only height and mean of GPET
- Fix BG function and remaining GPET pars from 1<sup>st</sup> time fitting
  
- Toy-MC study is done to estimate statistical error of cross section measurement

# Results



$E_{\text{cm}}$	$P(e^-, e^+)$	eff	$\Delta\sigma/\sigma$	S/B
350	(-0.8, +0.3)	$47.6 \pm 0.5\%$	$4.9 \pm 0.2\%$	$\sim 0.40$
	(+0.8, -0.3)	$47.8 \pm 0.5\%$	$5.0 \pm 0.2\%$	$\sim 0.75$
250	(-0.8, +0.3)	$66.4 \pm 0.5\%$	$3.6 \pm 0.1\%$	$\sim 0.37$
	(+0.8, -0.3)	$64.4 \pm 0.5\%$	$3.3 \pm 0.1\%$	$\sim 0.81$



# Plans

- Cut more BG without losing too much signal?
  - Improvement data selection : Implement **isolation** and **likelihood** cut?
- Study precision of fitted recoil **mass  $M_h$**
- Study **alternative polarization scenarios** e.g.  $(-0.8, 0)$ ,  $(+0.8, 0)$  ...etc

qqh  
@250GeV

By T. Tomita from Kyushu University

# Motivation

- In recoil mass study, leptonic channel such as  $Z \rightarrow ee, \mu\mu$  has very good signal/BG ratio.
- But the branching ratio of  $Z \rightarrow$ leptonic is  $\sim 3.5\%$  for each generation.



- In contrast, the branching ratio of  **$Z \rightarrow$ hadronic is  $\sim 70\%$ .**
- However, analysis is challenging due to a large amount of BG and worse Z mass resolution.

# Cut

- Box cut – targeted ZZ/WW hadronic event
  - Using 4 jet clustering
- Mass cut – targeted semi-leptonic event
  - Using 2 jet clustering
- Z like jet pt cut – targeted back to back Z event
- dijet mass cut – selected Z
  - Using y value clustering

$$y = \frac{2\min(E_i^2, E_j^2)(1 - \cos \theta_{ij})}{Q^2}$$

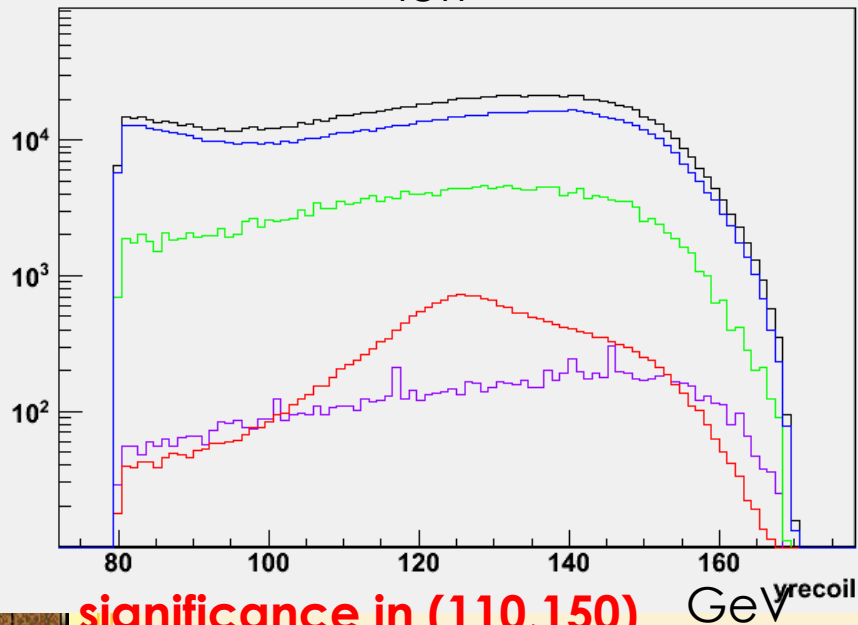
# Cut Table

cut	qqH	4 fermion	2 fermion	others
left	490,370	6M	16M	21M
right	331,118	798,363	10M	21M
Box cut (81,101) ZZ, (70,90) WW	82.7%	83.9%	99.0%	99.9%
Z like Jet pt > 20	70.6%	60.9%	30.3%	2.4%
dijet mass (76,106)	54.7%	36.2%	10.0%	0.7%
recoil mass (110,150)	43.1%	10.8%	2.7%	0.3%
Sphericity > 0.1	39.1%	6.7%	0.7%	0.2%
Thrust cut major>0.3, minor>0.1	36.9%	5.2%	0.4%	0.05%

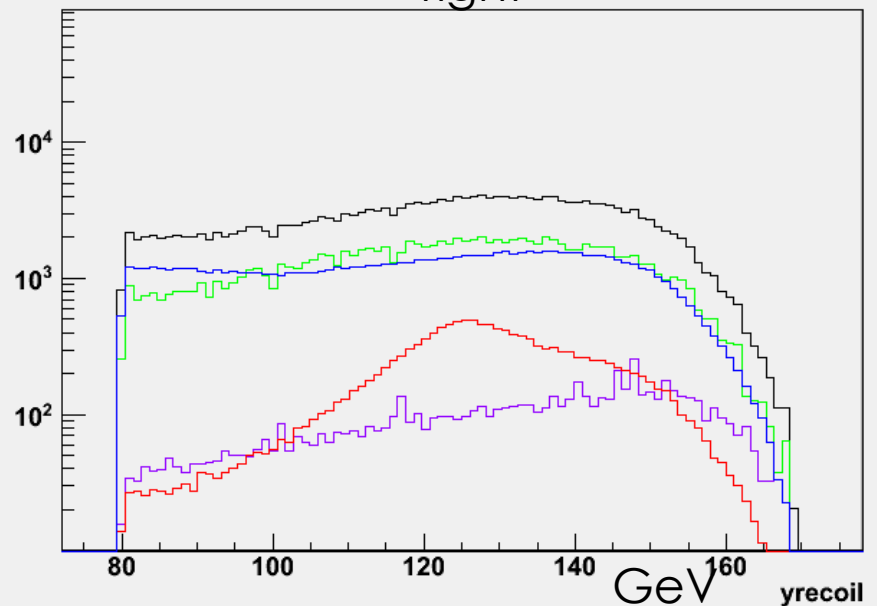
# results

2-fermion  
4-fermion  
signal(qqH)  
others

left



right



significance in (110,150) GeV

polarization	significance	$\Delta \sigma / \sigma$
left (-0.8, +0.3)	$20.5 \sigma$	4.8%
right (+0.8, -0.3)	$31.1 \sigma$	3.2%

# Summary & Prospects

- Right handed polarization shows better significance than left handed one.
- Especially in left handed polarization, **4 fermion background** should be reduced much more.
- We plan to categorize the events to analyze qqH channel **model independently**.
- We are preparing **ISR finder** and **Tau tagger** for categorization.

# Summary of Recoil Study

- The recoil mass technique is important feature at the ILC to measure Higgs mass and cross section of Zh event.

$\mu\mu h, eeh$ @250GeV		$\mu\mu h$		$eeh$		combined	
		Left	Right	Left	Right	Left	Right
MI	cross section	4.2%	3.8%	6.0%	6.0%	3.4%	3.2%
	mass [MeV]	34	31	231	214	34	31
semi-MI	cross section	3.8%	\	5.6%	\	3.1%	\
	mass [MeV]	33		89		31	

$\mu\mu h$ @350GeV	Left handed	Right handed
cross section	4.9%	5.0%
cross section (250GeV)	3.6%	3.3%

$qqh$ @250GeV	Left handed	Right handed
cross section	4.8%	3.2%



# Backup Slides

# Lepton Selection

- **Muon (electron) selection**

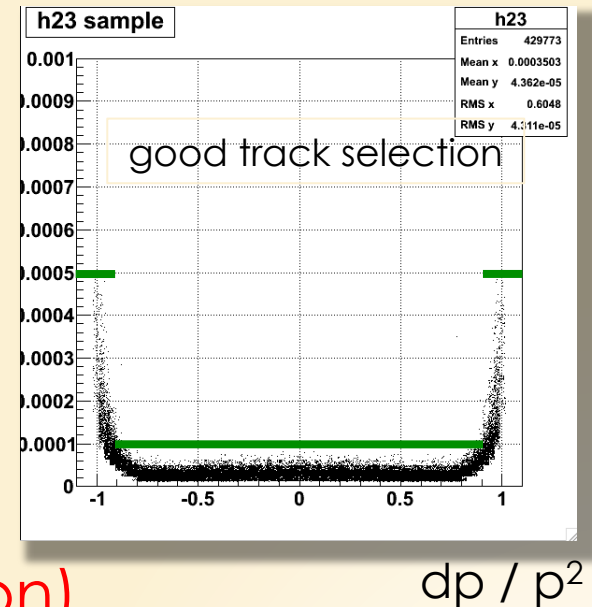
- Momentum  $p > 15$  [GeV]
- Small (Large) energy deposited in calorimeters
  - $E_{\text{ecal}} / E_{\text{total}} < 0.5$  ( $> 0.6$ )
  - $E_{\text{total}} / p_{\text{track}} < 0.3$  ( $> 0.9$ )

- **Good track selection**

- Track with small error (different selections between polar angle of tracks, barrel or end cap)
  - $dp / p^2 < 2.5 \times 10^{-5} \oplus 8 \times 10^{-4} / p$   
(for  $\cos\theta < 0.78$ )
  - $dp / p^2 < 5 \times 10^{-4}$   
(for  $\cos\theta > 0.78$ )

- **Impact parameter (only for muon)**

- To suppress muons from tau decays which tend to have large impact parameters.  
 $D_0 / dD_0 < 5$

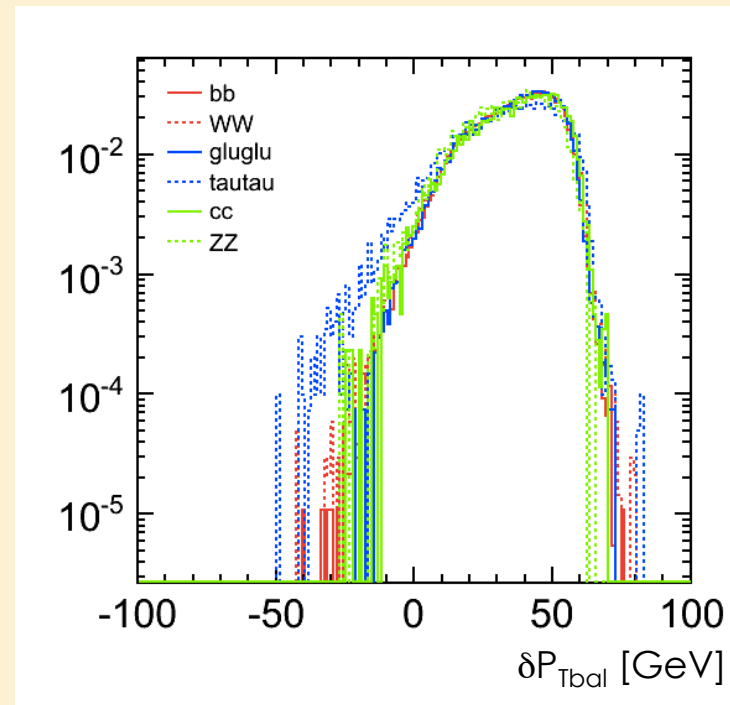


# BG Rejection and Cut Table

$\mu\mu h$	signal	ll	llvv	llff	others
No Cut	2603	3.2M	507166	390041	7.1M
selection	2278	17200	16286	7874	70
$P_{Tdl}$	2161	9965	14095	6852	59
$M_{dl}$	2036	7891	8147	5808	37
acop	1903	6825	7659	5306	33
$dP_{Tbal}$	1894	1751	7518	5189	33
$\cos\theta_{missing}$	1882	1257	7517	4815	30
$M_{recoil}$	1730	536	3116	1575	12
Likelihood	1386	322	1479	1054	3
eeh	signal	ll	llnn	llff	others
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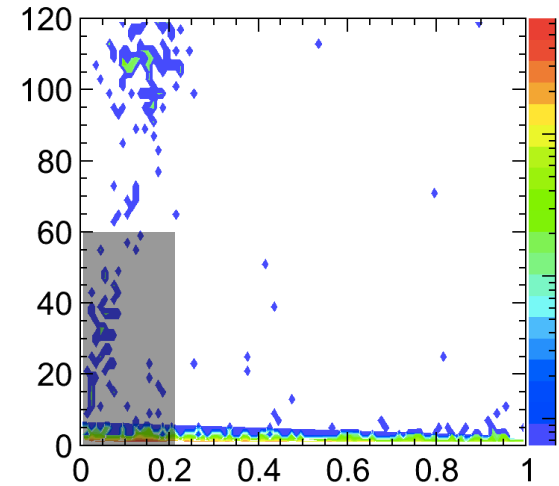
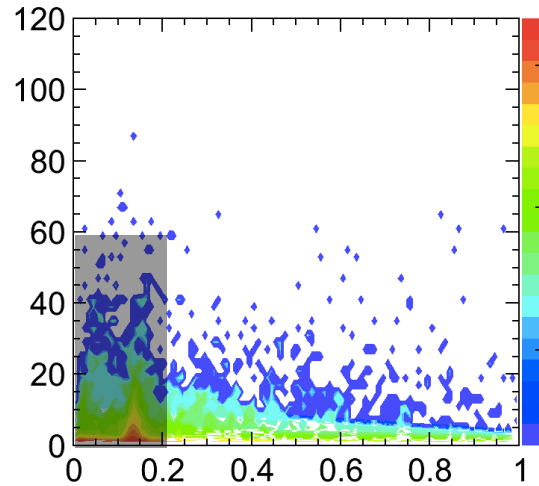
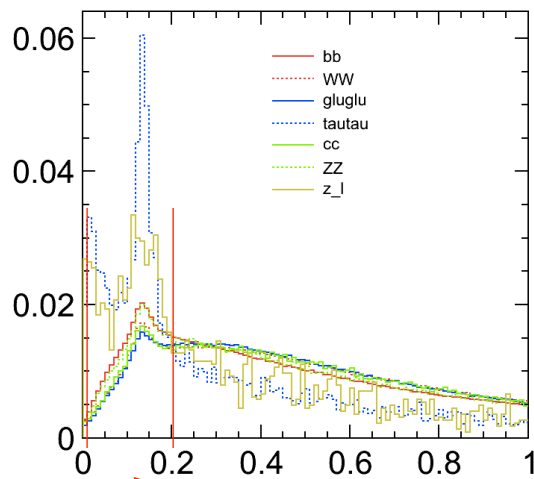
# Bias Suppression (for $\delta P_{Tbal}$ )

- In  $\delta P_{Tbal}$  selection, we look at other particles (photon) besides di-lepton :
- $$\delta P_{Tbal} \equiv PT_{dl} - PT_{\gamma}$$
- So there is bias for some Higgs decay mode ( $h \rightarrow \tau\tau$  mode).



# Bias Suppression (for $\delta P_{Tbal}$ )

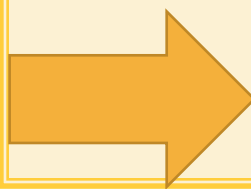
- We can suppress this bias using **Energy** of photon and **invariant mass** of each photon



In  $h \rightarrow \tau\tau$ , there is a peak at  $m_{2\gamma} \sim m_{\pi}$

$h \rightarrow \tau\tau$  signal

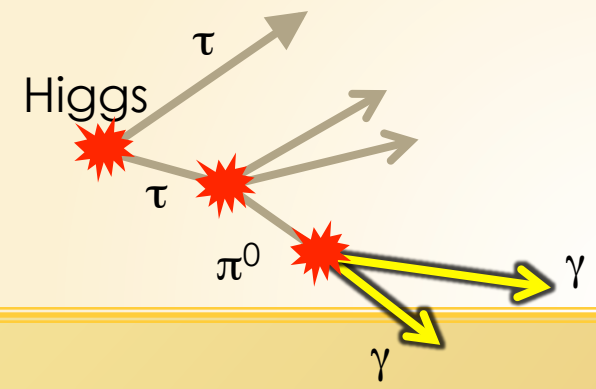
$l\gamma$  BG



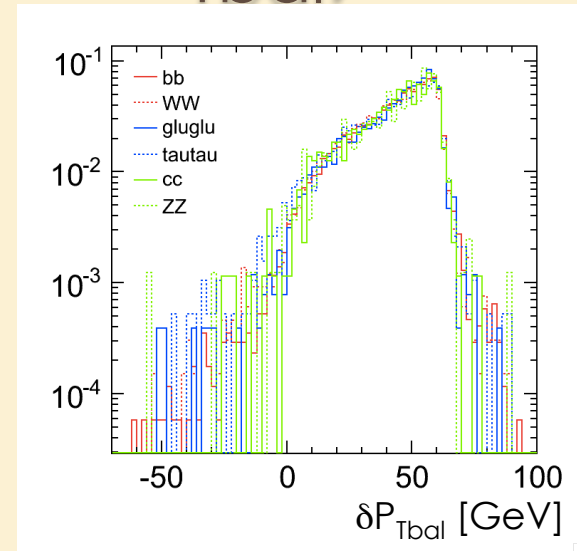
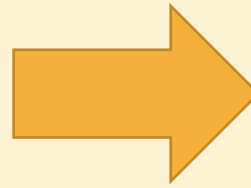
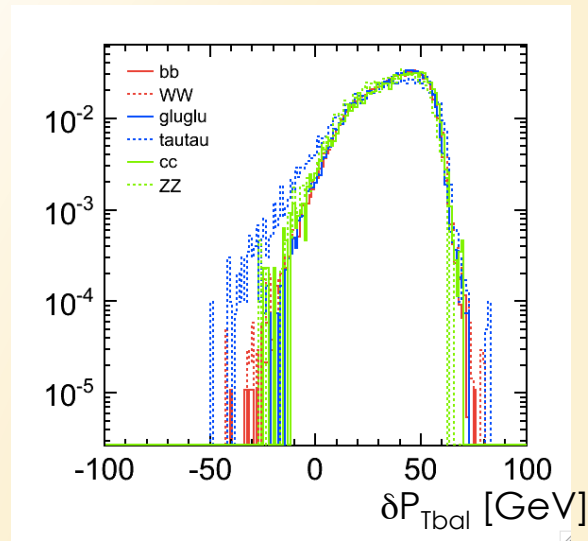
condition of used  $\gamma$

$m_{2\gamma} > 0.2$  [GeV]

or  $E_{\gamma} > 60$  [GeV]



# Bias Suppression (for $\delta P_{Tbal}$ )



**Comparison  
old&new**

**efficiency of  $dP_{Tbal}$  cut**

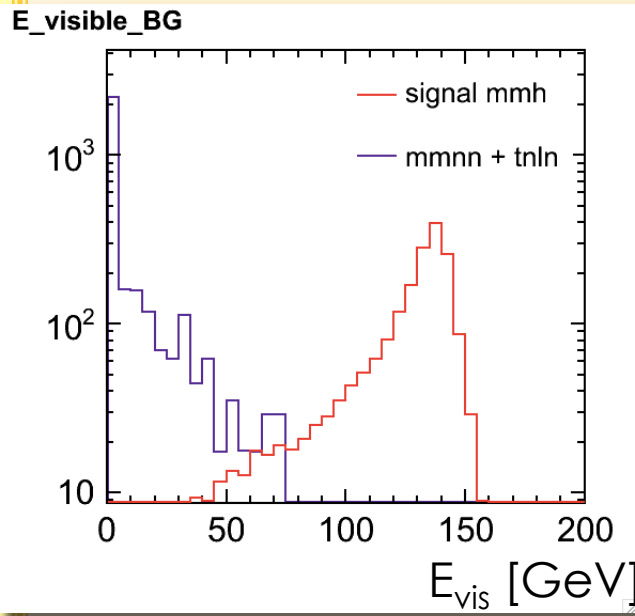
	bb	$\tau\tau$	cc	z_l (BG)
Simple calc.	99.4%	95.3%	99.0%	14.5%
My calc.	99.8%	97.8%	99.6%	22.2%

In new calculation of  $\delta P_{Tbal}$ , bias will decrease.

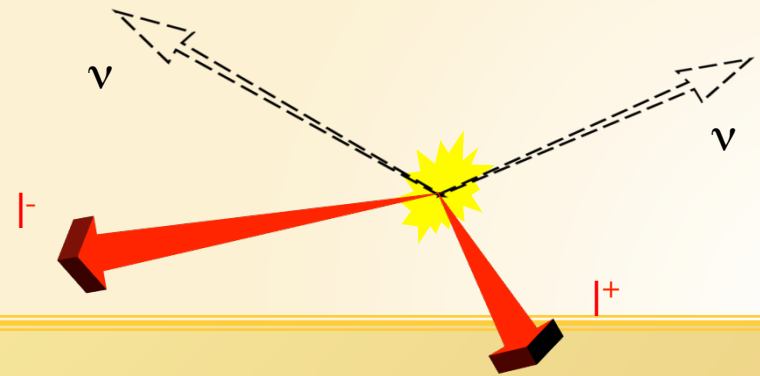
# Semi-MI Analysis

$\mu\mu h$	signal	ll	llnn	llff	others
After Cut	1386	322	1479	1054	3
		ll	llnn	llff	others
		1496	2203	937	4

There seems to be large number of remaining llvv BG.



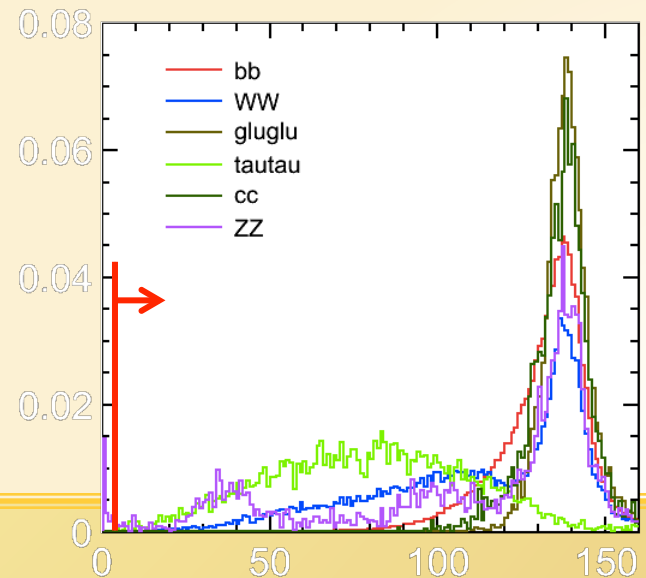
- Since contribution from Higgs invisible decays can be calibrated with data, visible energy selection is effective for reducing these BG.
- $E_{vis} := E_{PFOs} - E_{di-lepton} > 5 \text{ [GeV]}$
- Loose selection is applied to avoid bias in signal selection.



# Efficiency of $E_{\text{visible}}$

H decay mode	$\mu\mu h$ ( $E_{\text{vis}}$ eff.)	After all cut	$eeh$ ( $E_{\text{vis}}$ eff.)	After all cut
bb	100%	66.31%	98.68%	39.14%
WW	100%	66.00%	98.31%	38.67%
gluglu	100%	65.40%	98.67%	38.82%
$\tau\tau$	99.94%	65.66%	98.43%	37.82%
cc	100%	66.32%	98.25%	39.43%
ZZ	96.64%	63.98%	94.84%	37.90%

- Bias as expected from SM.





# qqh Cut Table

cut	qqh	4 fermion	2 fermion	others (aa, 1f_3f, etc..)
left	490,370	6,255,904	16,267,218	21,274,095
right	331,118	798,363	10,355,564	21,274,095
Box cut (81,101) ZZ (70,90) WW	82.7%	83.9%	99.0%	99.9%
Z like Jet pt cut pt > 20	70.6%	60.9%	30.3%	2.4%
dijet mass cut (76,106)	54.7%	36.2%	10.0%	0.7%
recoil mass cut (110,150)	43.1%	10.8%	2.7%	0.3%
Sphericity cut > 0.1	39.1%	6.7%	0.7%	0.2%
Thrust cut major>0.3 minor>0.1	36.9%	5.2%	0.4%	0.05%